

Measuring Transverse Quark Polarization with Spin Dependent Fragmentation Functions at



and



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and Matter



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Outline

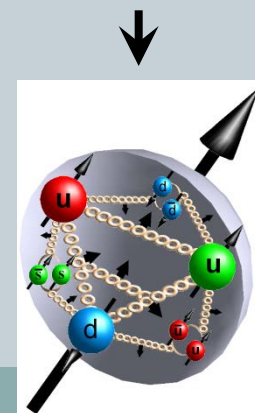
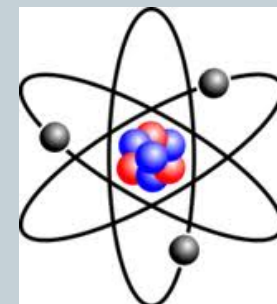
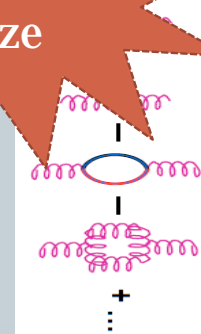
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- **Motivation: Measuring Transversity of the Nucleon**
 - Transversity
 - Need for transverse spin dependent fragmentation functions for quark polarimetry
- **Transverse spin dependent Fragmentation Function measurement in e^+e^- annihilation at Belle**
 - The Belle Experiment
 - Recent Results for di-Hadron Interference Fragmentation Function
 - Extraction of Transversity
- **Outlook**
 - Future Fragmentation Function measurements at Belle I+II

Motivation for Studying Spin Proton Structure & Quantum Chromodynamics

Millennium
Prize

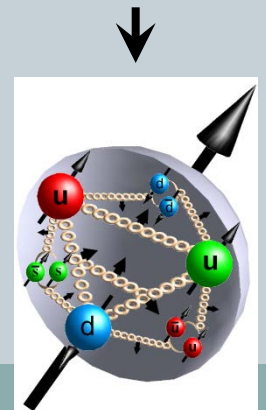
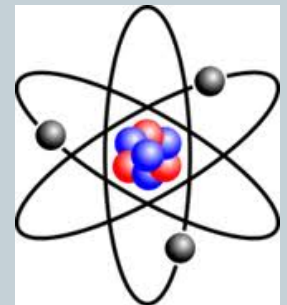
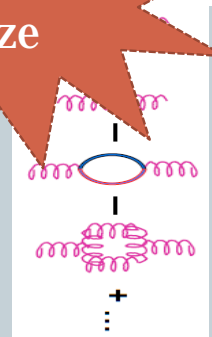
- QCD successful in describing high energy reactions
- **BUT** No consistent description of hadronic sector
 - → No consistent description of fundamental bound state of the theory
 - QCD binding energy : most of the visible mass in the universe
 - Spin is fundamental Quantum Number: What role does it play? Use transverse spin as precision probe.



Motivation for Studying Spin Proton Structure & Quantum Chromo Dynamics

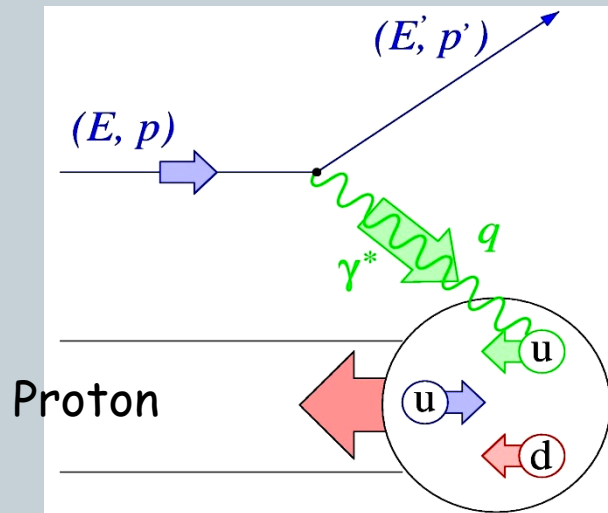
Millennium
Prize

- QCD successful in describing high energy reactions
- **BUT** No consistent description of hadronic sector
 - → No consistent description of fundamental bound state of the theory : proton
 - QCD binding energy : most of the visible energy in the universe
 - Spin is fundamental Quantum Number: What role does it play? Use transverse spin as precision probe
- Compare to QED:
 - Bound state: QED: atom
 - Stringent tests of QED from study of **spin** structure of hydrogen
 - ✦ Lamb shift (Nobel prize 1955)
 - → Atomic physics, QCD?



Probes to Study Polarized Proton Structure

Inclusive polarized deep inelastic scattering (DIS)



The diagram shows a virtual photon γ^* (represented by a black wavy arrow) interacting with a quark in a proton. The photon has a helicity $m = +1$ (indicated by a black arrow). The quark is shown with a spin state $m = +1/2$ (indicated by a pink arrow). The quark is represented by a circle containing two quarks: an up quark (u) with a blue arrow pointing right and a down quark (d) with a red arrow pointing left. The quark that interacts with the photon is shown with a green arrow pointing right, indicating its spin state.

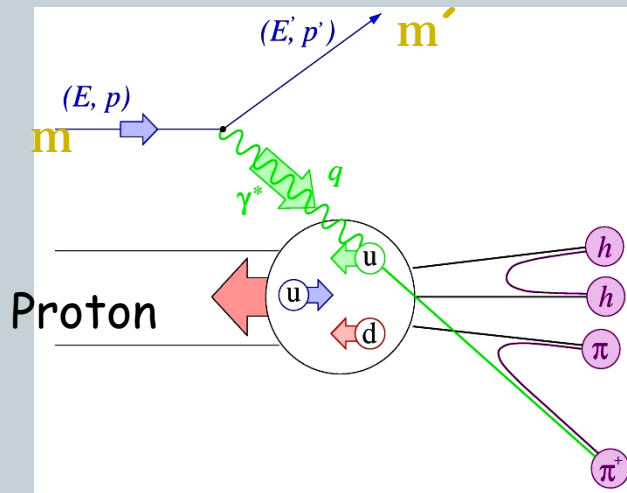
$$\sigma_{1/2} \sim \sum_i e_i^2 q_i^+$$

The diagram shows a virtual photon γ^* (represented by a black wavy arrow) interacting with a quark in a proton. The photon has a helicity $m = +1$ (indicated by a black arrow). The quark is shown with a spin state $m = -1/2$ (indicated by a pink arrow). The quark is represented by a circle containing two quarks: an up quark (u) with a blue arrow pointing right and a down quark (d) with a red arrow pointing left. The quark that interacts with the photon is shown with a green arrow pointing left, indicating its spin state.

$$\sigma_{3/2} \sim \sum_i e_i^2 q_i^-$$

Probes to Study Polarized Proton Structure

Semi-Inclusive polarized deep inelastic scattering (DIS)



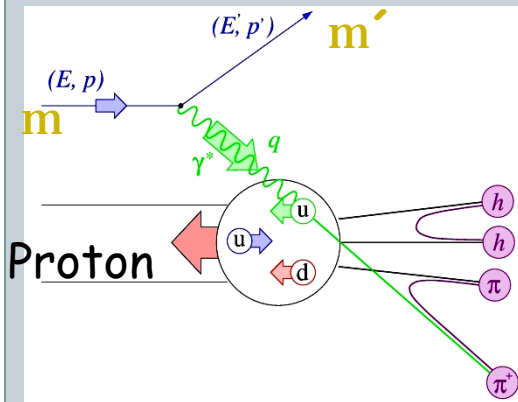
Fragmentation Process:
Outgoing quark forms hadrons

$$\sigma_{1/2} \sim \sum_i e_i^2 q_i^+$$

$$\sigma_{3/2} \sim \sum_i e_i^2 q_i^-$$

Probes to Study Polarized Proton Structure

(semi) Inclusive polarized deep inelastic scattering (DIS)



polarized pp scattering

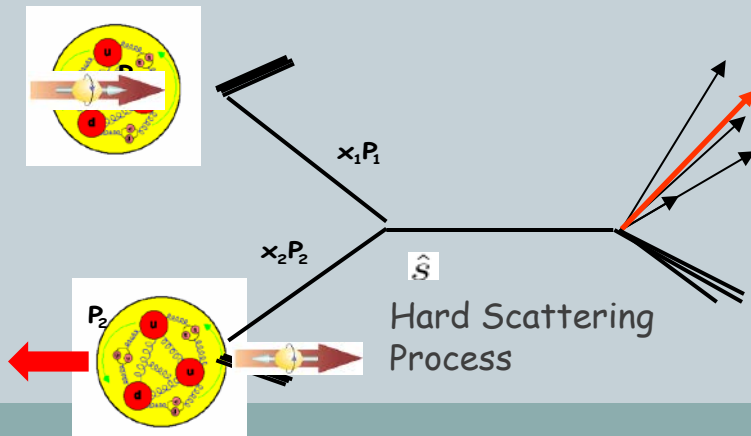


Diagram showing a virtual photon γ^* with helicity $m = +1$ interacting with a proton with helicity $m = -1/2$. The interaction is represented by a circle containing a red circle with a minus sign and a blue circle with a plus sign. The resulting cross-section is given by:

$$\sigma_{1/2} \sim \sum_i e_i^2 q_i^+$$

Diagram showing a virtual photon γ^* with helicity $m = +1$ interacting with a proton with helicity $m = +1/2$. The interaction is represented by a circle containing a red circle with a minus sign and a blue circle with a plus sign. The resulting cross-section is given by:

$$\sigma_{3/2} \sim \sum_i e_i^2 q_i^-$$

Three Feynman diagrams representing different scattering processes:

- ΔG^2
- $\Delta G \Delta q$
- Δq^2

Dominates at RHIC

Parton Distribution Functions

The three leading order, collinear PDFs

$f_1^q(x)$

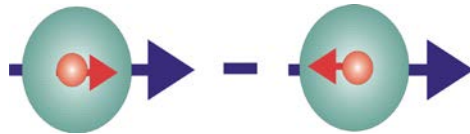


unpolarized PDF

quark with momentum $x=p_{quark}/p_{proton}$ in a nucleon

well known – unpolarized DIS

$g_1^q(x)$

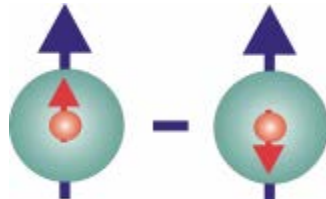


helicity PDF

quark with spin parallel to the nucleon spin in a longitudinally polarized nucleon

known – polarized DIS

$h_1^q(x)$



transversity PDF

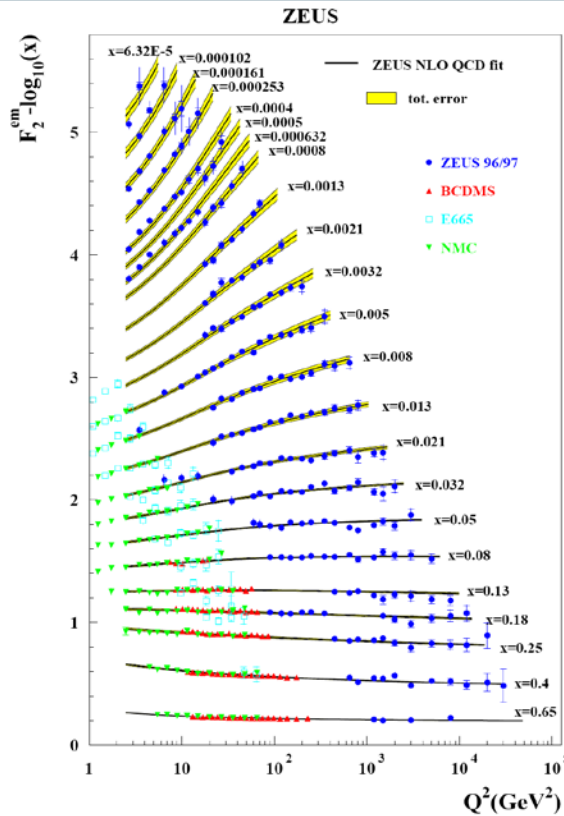
quark with spin parallel to the nucleon spin in a transversely polarized nucleon
Helicity – transversity: measurement of the nonzero angular momentum components in the protons wavefunction

*chiral odd, poorly known
Cannot be measured inclusively*

Current Status of Distribution Functions

$$f_1 = \bullet$$

Unpolarized



$$F_2 \propto \sum_q e^q f_1^q$$

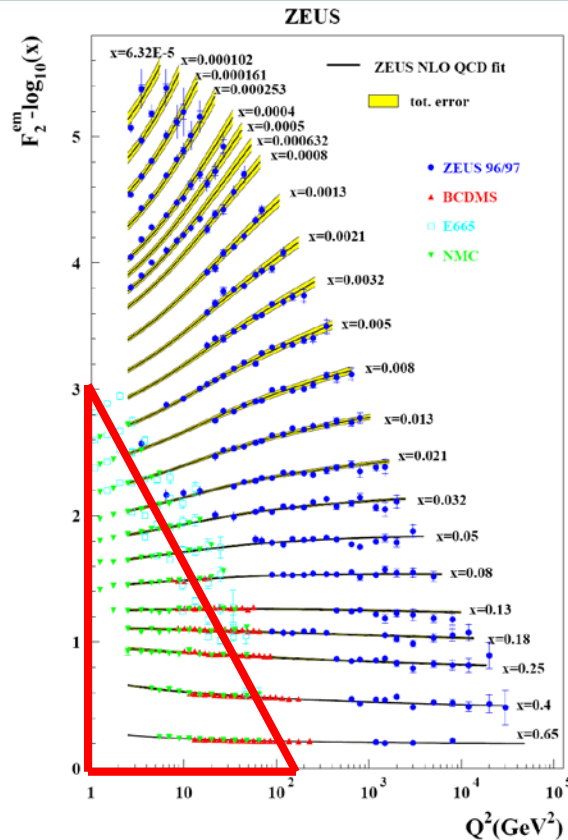
Current Status of Distribution Functions

$$f_1 = \bullet$$

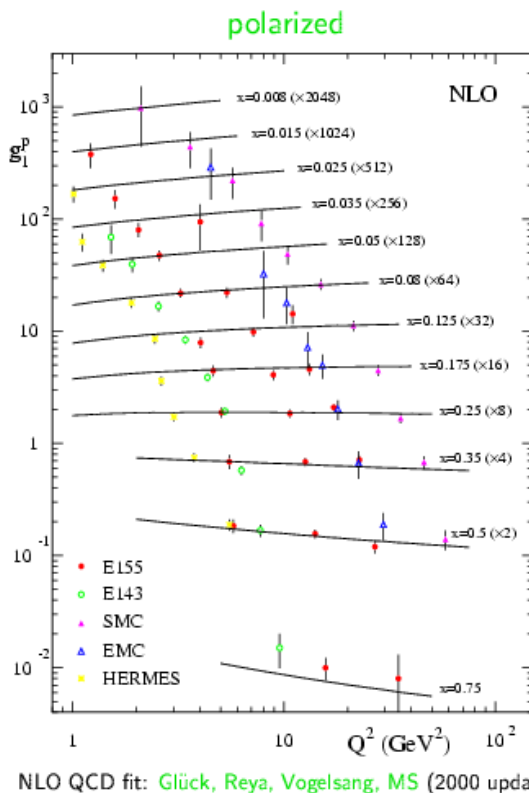
Unpolarized

$$g_1 = \bullet \rightarrow \rightarrow - \bullet \rightarrow \rightarrow$$

Longitudinally Polarized



$$F_2 \propto \sum_q x e_q^2 f_1^q$$



$$g_1 \propto \sum_q e_q^2 g_1^q$$

Current Status of Distribution Functions

$$f_1 = \bullet$$

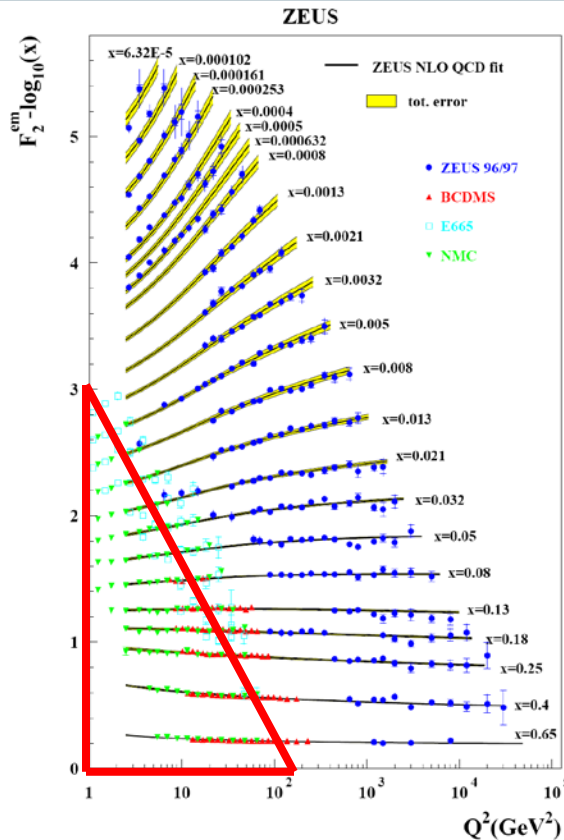
Unpolarized

$$g_1 = \bullet \rightarrow - \bullet \rightarrow$$

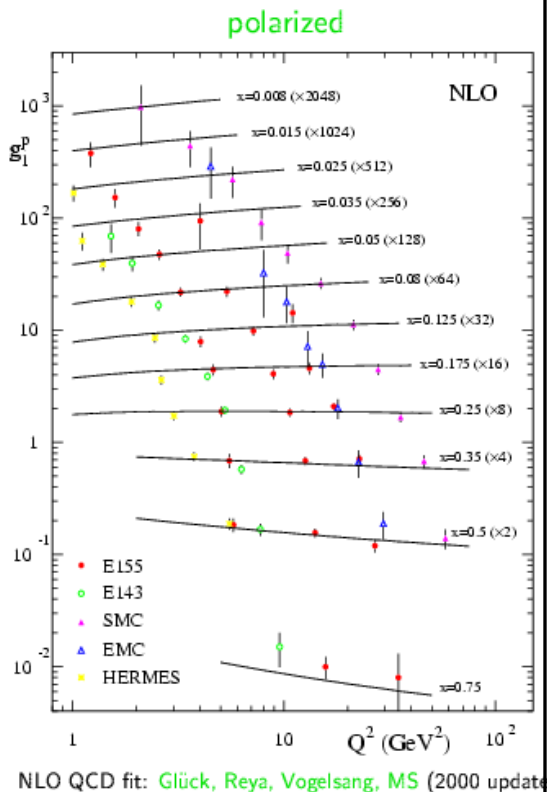
Longitudinally Polarized

$$h_1 = \begin{array}{c} \uparrow \\ \bullet \\ \downarrow \end{array} - \begin{array}{c} \uparrow \\ \bullet \\ \uparrow \end{array}$$

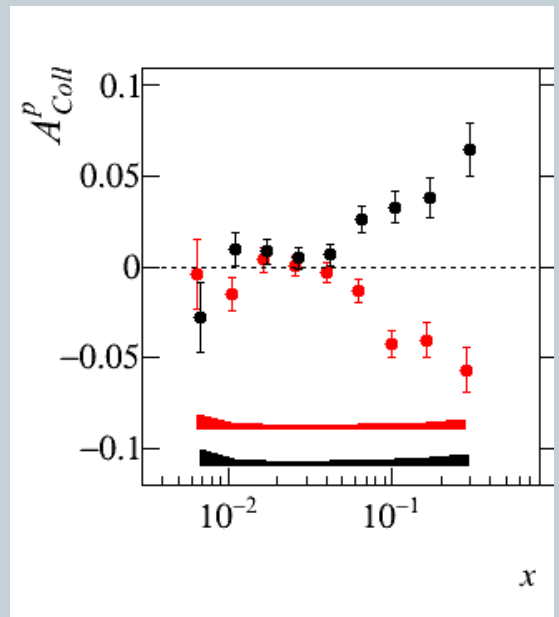
Transversely Polarized



$$F_2 \propto \sum_q x e_q^2 f_1^q$$



$$g_1 \propto \sum_q e_q^2 g_1^q$$



A_{Collins}^p

$$\propto \frac{\sum_q e_q^2 h_1^q(x) * H_1^\perp}{\sum_q e_q^2 q_1^q(x) D_q^h(z)}$$

Chiral odd -
cannot be measured inclusively

Current Status of Distribution Functions

$$f_1 = \bullet$$

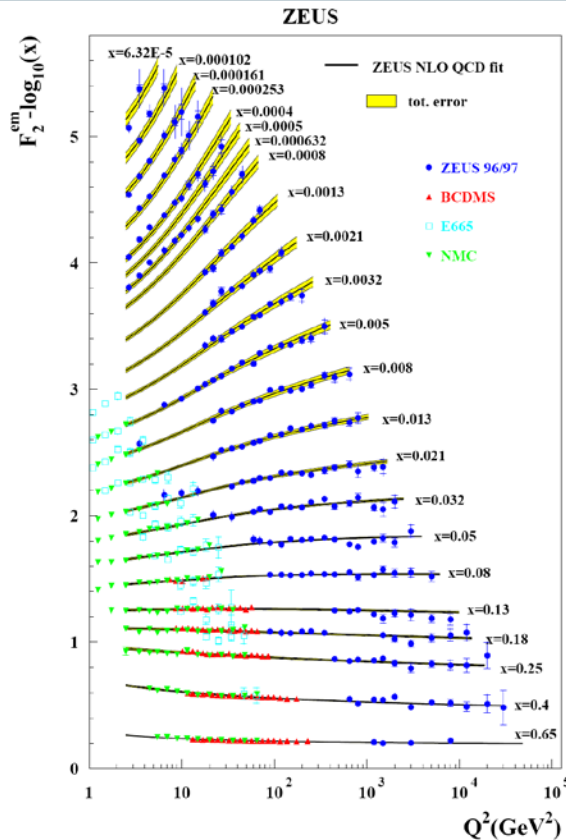
Unpolarized

$$g_1 = \bullet \rightarrow - \bullet \rightarrow$$

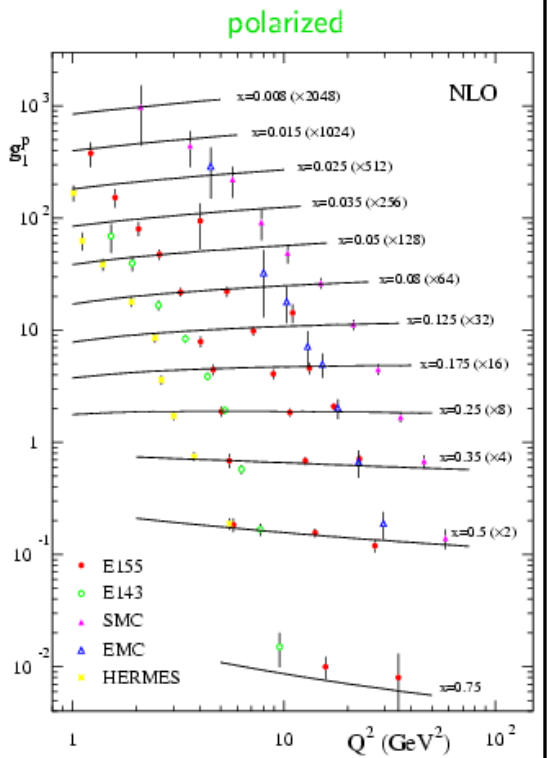
Longitudinally Polarized

$$h_1 = \begin{array}{c} \uparrow \\ \bullet \\ \downarrow \end{array} - \begin{array}{c} \uparrow \\ \bullet \\ \downarrow \end{array}$$

Transversely Polarized

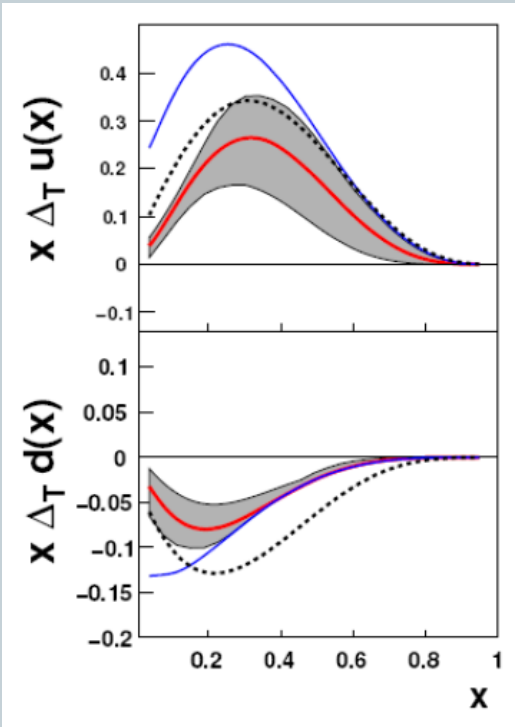


$$F_2 \propto \sum_q x e_q^2 f_1^q$$



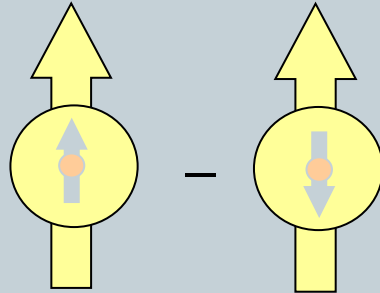
NLO QCD fit: Glück, Reya, Vogelsang, MS (2000 update)

$$g_1 \propto \sum_q e_q^2 g_1^q$$



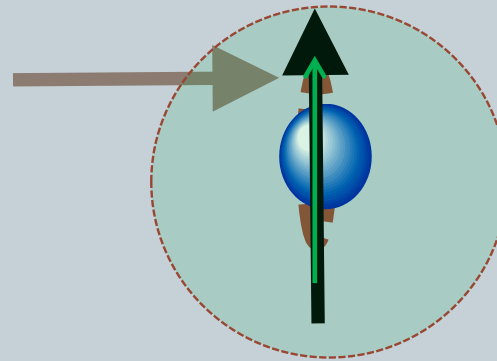
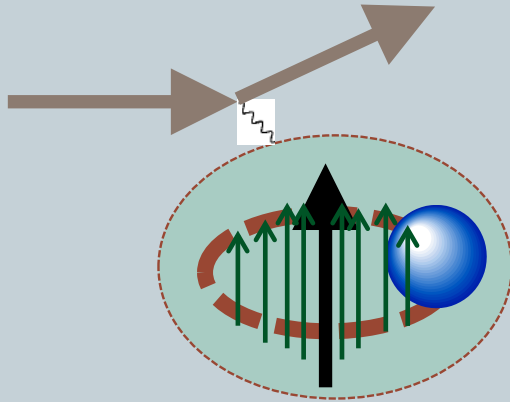
Transversity:

Why is

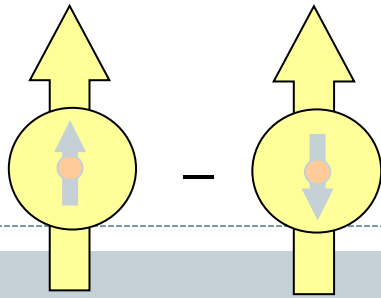


so hard to measure?

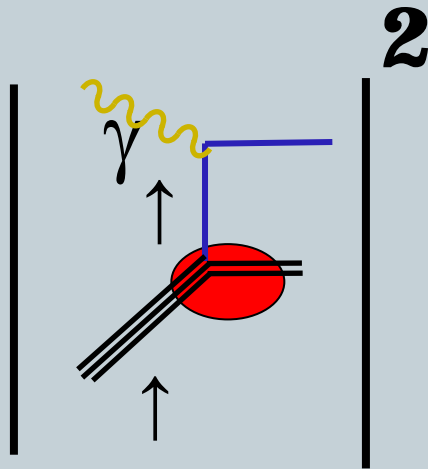
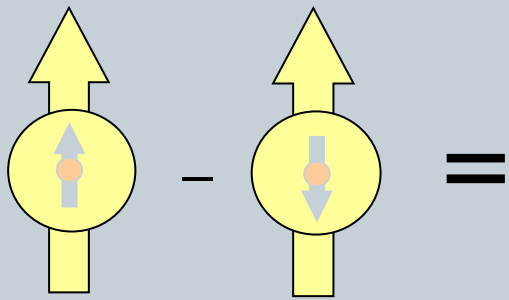
- Naïve picture: leptonic probe too 'fast' to be sensitive to transverse polarization



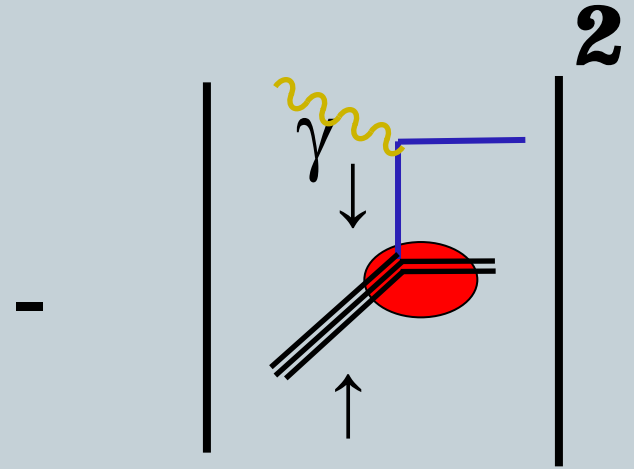
Why is



so hard to measure?

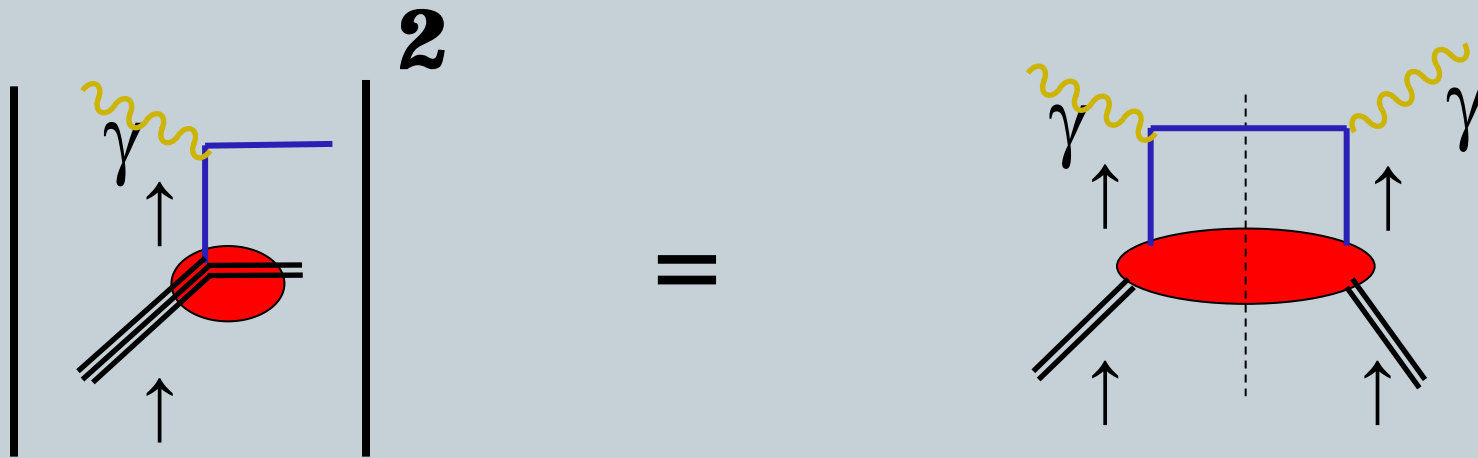


Probability of finding \uparrow quark



Probability of finding \downarrow quark

Handbag Diagrams



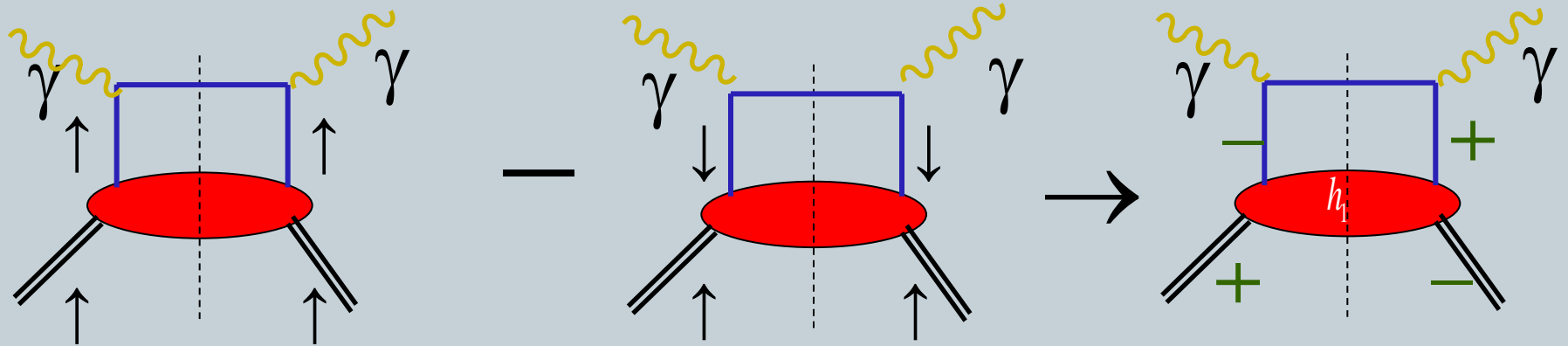
Optical Theorem:

$$\sigma = -\text{Im}(A_{\text{forward scattering}})$$

Transversity is Chiral Odd



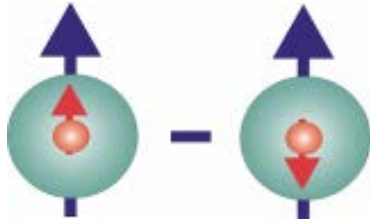
- **Transversity base:**



- **Helicity base:** chiral odd
- Needs chiral odd partner \rightarrow Fragmentation Function
- Does not couple to gluons \Rightarrow different QCD evolution than $g_1(x)$
- Dominated by Valence Region

Importance of Transversity

$h_1^q(x)$

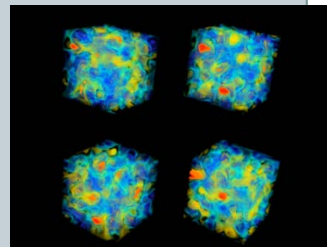


$$\frac{1}{2} = \frac{1}{2} \sum_{q, \bar{q}} \int dx h_q(x) + \sum_{q, \bar{q}, G} \langle L_{ST} \rangle$$

Baker, Leader, Trueman:
Transverse Polarization Sum Rule

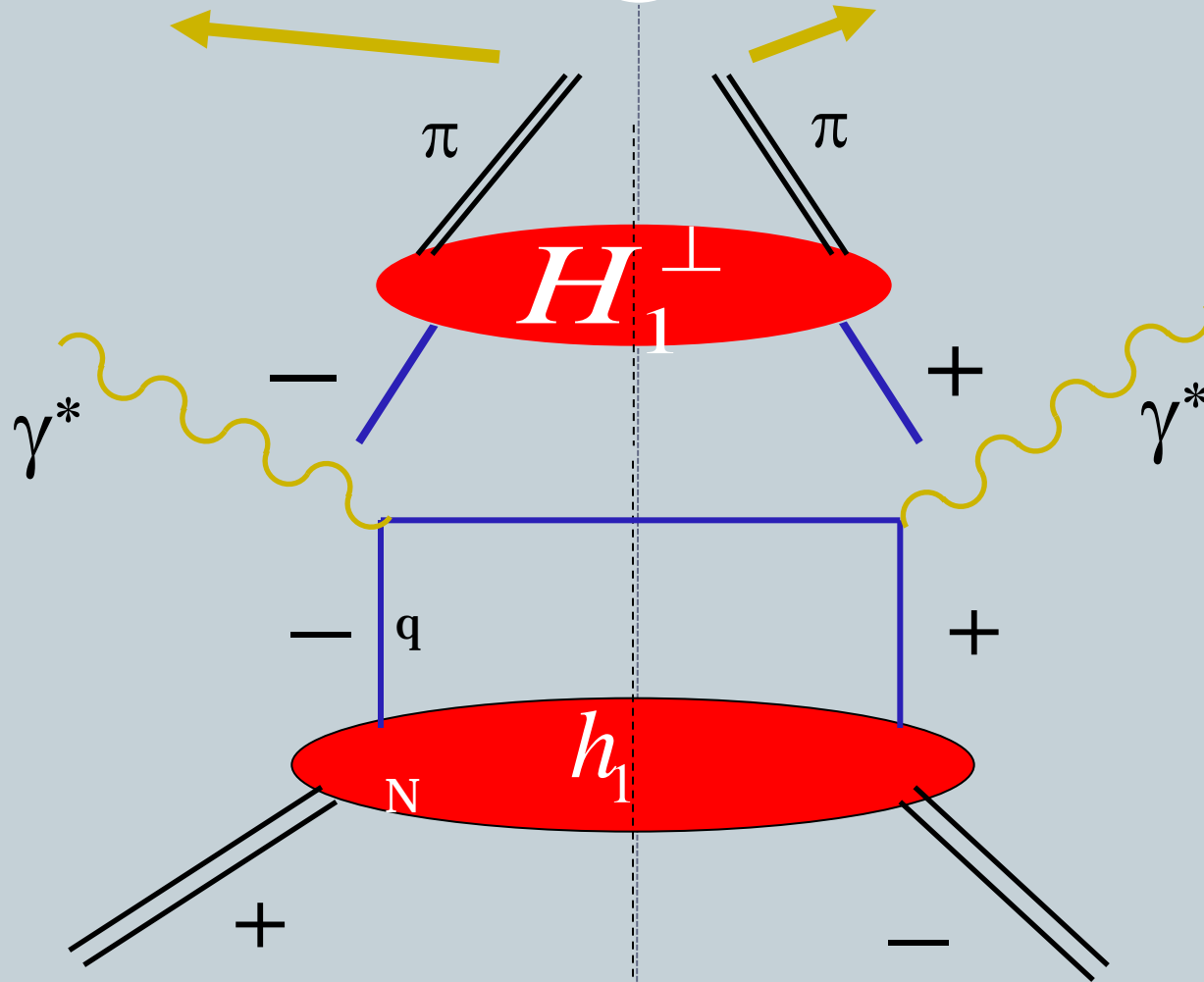
Only way to access tensor charge: $\langle |\sigma^{\mu\nu}| \rangle = \int dx (h_q(x) - h_{\bar{q}}(x)) = g_T$

- **Tensor charge g_T can come from lattice and experiment**
 - Parton distributions on the light-cone \rightarrow compare moments
- Allows first order calculations connection to experiment
- Other quantities from lattice: Quark orbital momentum etc



Chiral odd Fragmentation Functions

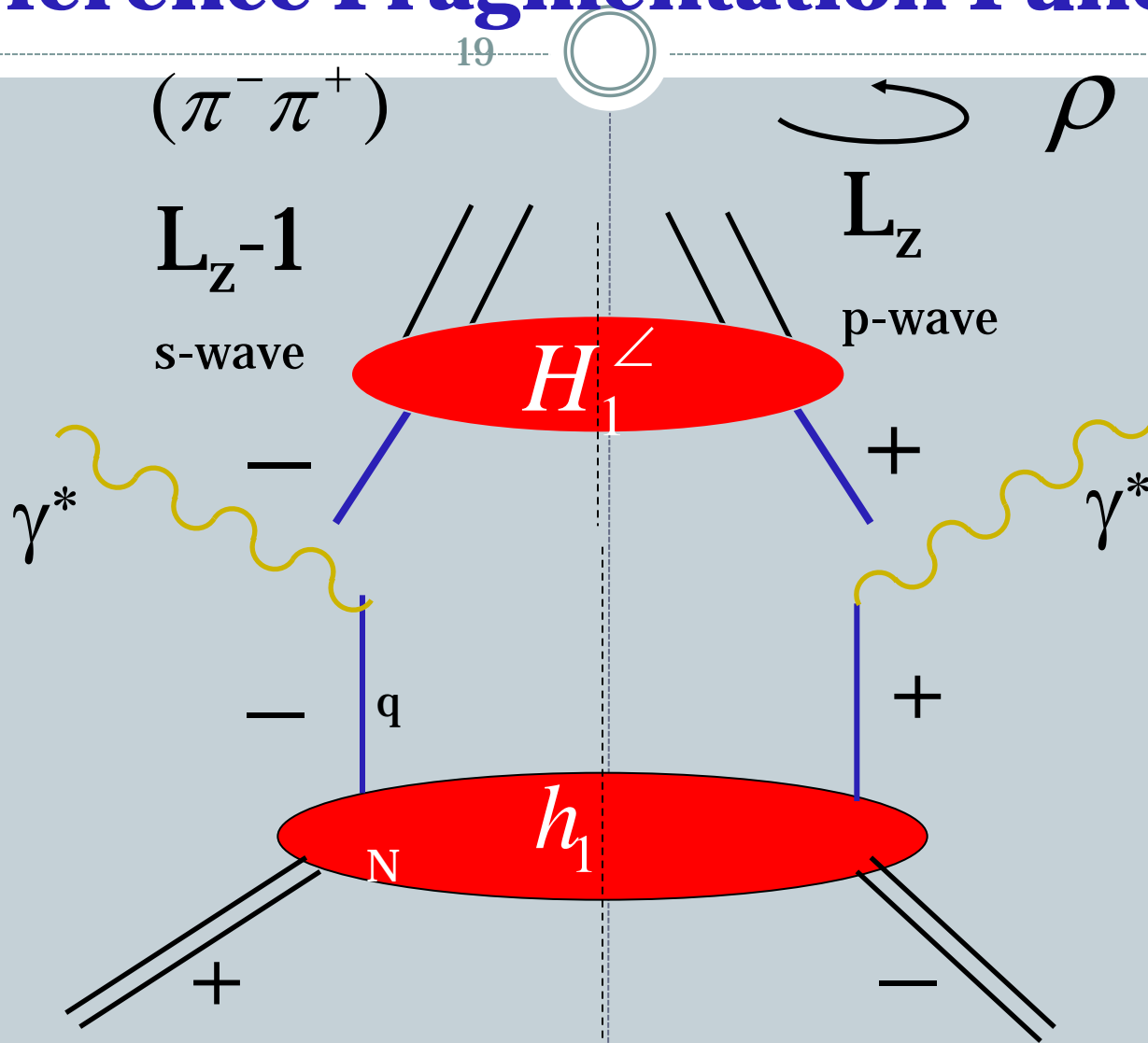
Collins effect



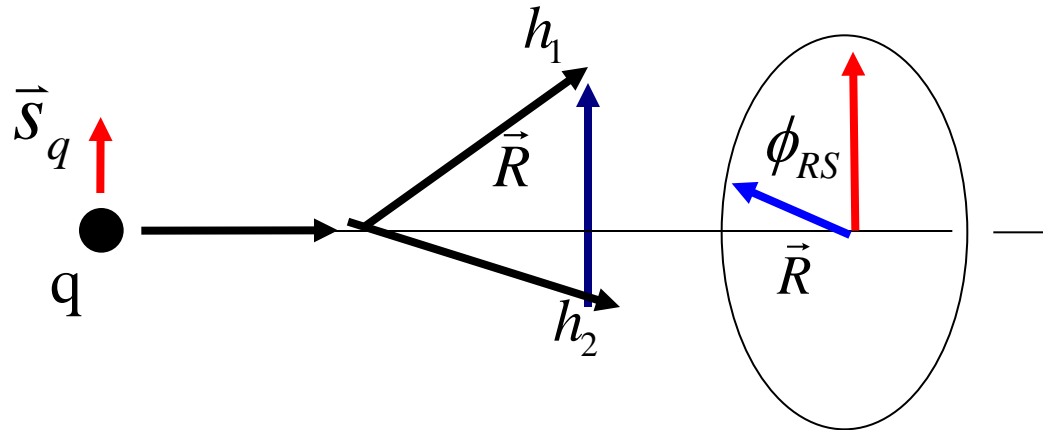
H_1^\perp : Collins FF

Chiral odd FFs

Interference Fragmentation Function



Quark Polarimetry with Interference FF in Quark Fragmentation



\vec{k} : quark momentum
 \vec{s}_q : quark spin
 \vec{R} : momentum difference $\vec{p}_{h1} - \vec{p}_{h2}$
 \vec{R}_T : transverse hadron momentum difference
 z_{pair} : relative hadron pair momentum
 $= 2E_{pair}/\sqrt{s}$
 m : hadron pair invariant mass

Interference Fragmentation Function:

Fragmentation of a transversely polarized quark q into two spin-less hadron $h1, h2$ carries an azimuthal dependence:

$$\propto (\vec{k} \times \vec{R}_T) \cdot \vec{s}_q$$

$$\propto \sin \phi_{RS}$$

Transversity from di-Hadron SSA

p+p c.m.s. = lab frame

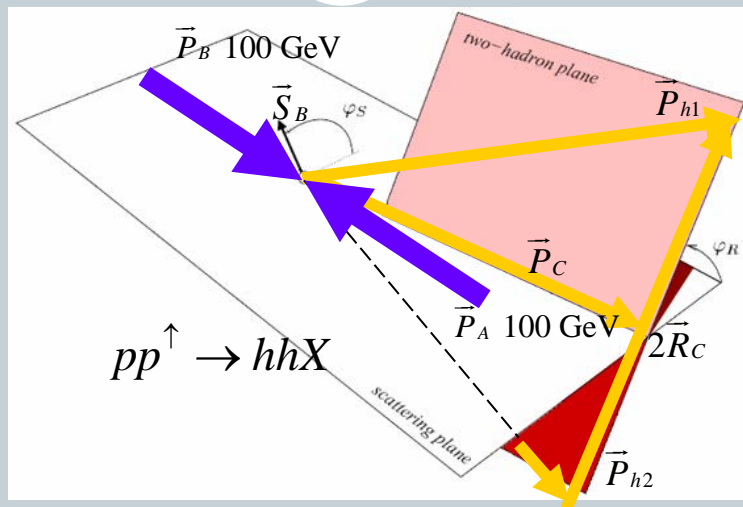
\vec{P}_A, \vec{P}_B : momenta of protons

$\vec{P}_{h1}, \vec{P}_{h2}$: momenta of hadrons

$\vec{P}_C = \vec{P}_{h1} + \vec{P}_{h2}$

$\vec{R}_C = (\vec{P}_{h1} - \vec{P}_{h2})/2$

\vec{S}_B : proton spin orientation



ϕ_R : from scattering plane
to hadron plane

ϕ_S : from polarization vector
to scattering plane

$$d\sigma_{UT} = 2 |\mathbf{P}_{C\perp}| \sum_{a,b,c,d} \frac{|\mathbf{R}_C|}{M_C} |\mathbf{S}_{BT}| \sin(\phi_{S_B} - \phi_{R_C}) \int \frac{dx_a dx_b}{16\pi z_c} f_1^a(x_a) h_1^b(x_b) \frac{d\Delta\hat{\sigma}_{ab\uparrow \rightarrow c\uparrow d}}{d\hat{t}} H_{1,ot}^{\lessgtr c}(\bar{z}_c, M_C^2)$$

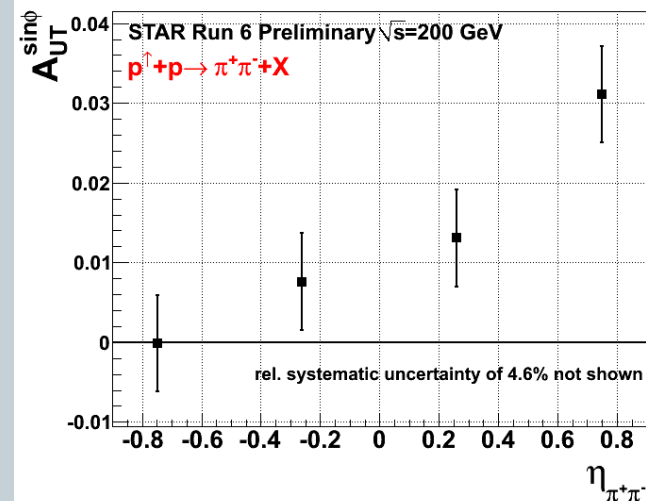
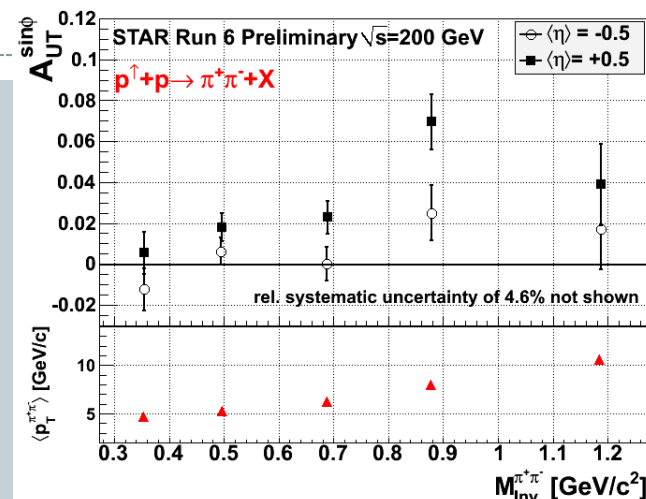
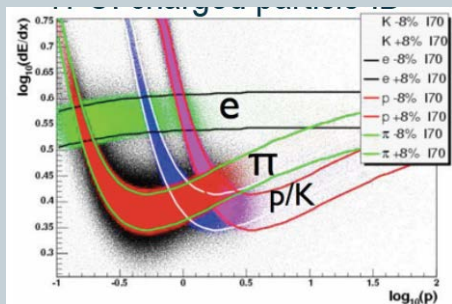
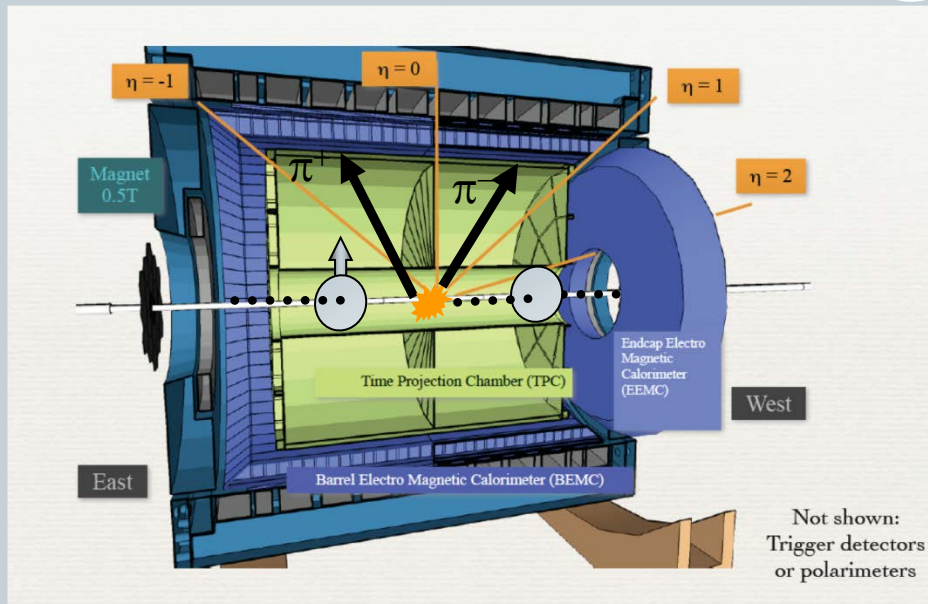
**Unpolarized
quark distribution**
Known from DIS

Transversity
to be extracted

**Hard scattering
cross section**
from pQCD

IFF + Di-hadron FF
measured in e+e at Belle-

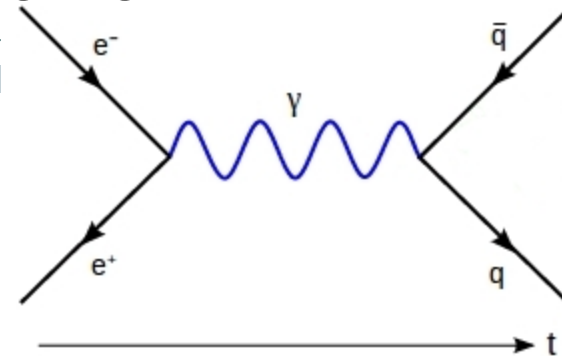
NEW: STAR shows significant Signal!



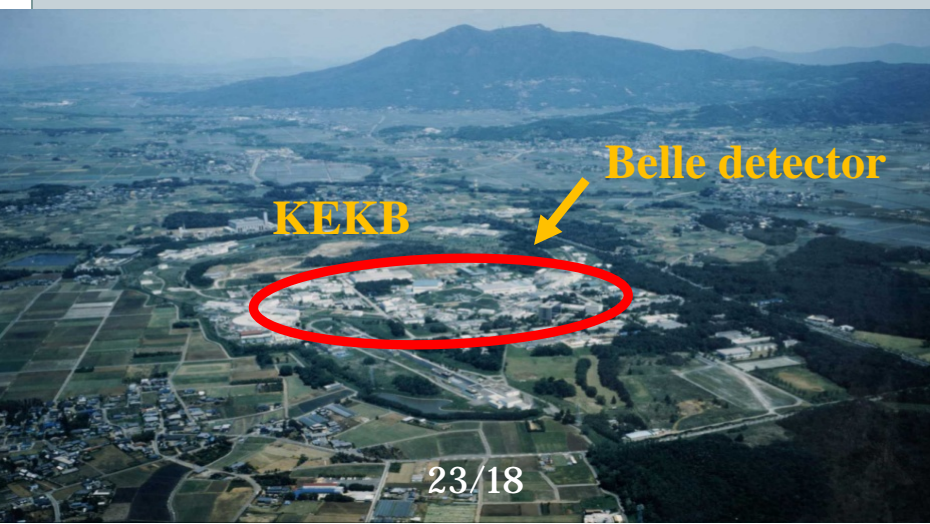
- First significant signal of transversity in polarized proton collisions

$$A_{UT} \propto h_1 \cdot H_1^<$$

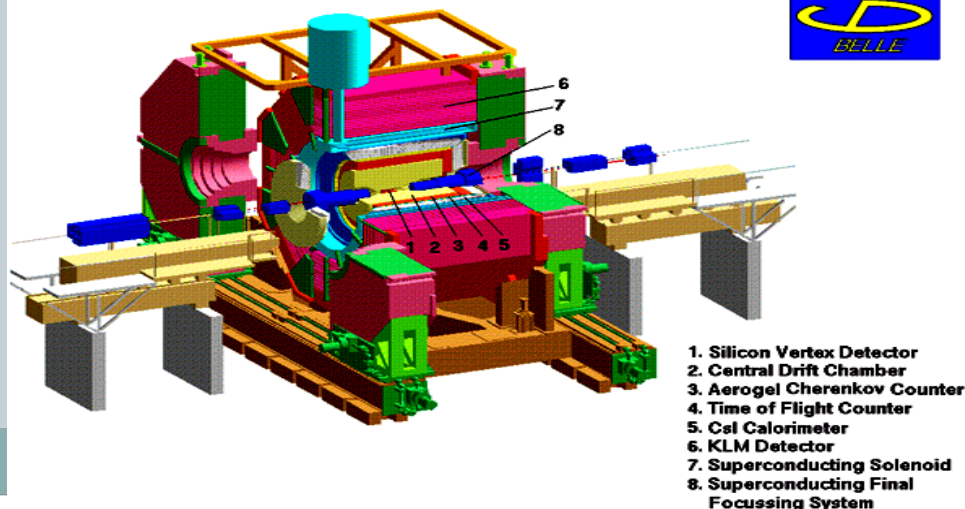
Measurements of Fragmentation Functions in e^+e^- at Belle



- KEK-B: asymmetric e^+ (3.5 GeV) e^- (8 GeV) collider:
 - $\sqrt{s} = 10.58 \text{ GeV}$, $e^+e^- \rightarrow Y(4S) \rightarrow B \bar{B}$
 - $\sqrt{s} = 10.52 \text{ GeV}$, $e^+e^- \rightarrow q\bar{q}$ (u,d,s,c) 'continuum'
- ideal detector for high precision measurements:
 - tracking acceptance θ [17° ; 150°]: Azimuthally symmetric
 - particle identification (PID): dE/dx , Cherenkov, ToF, EMcal, MuID
- Available data:
 - $\sim 1.8 \cdot 10^9$ events at 10.58 GeV,
 - $\sim 220 \cdot 10^6$ events at 10.52 GeV

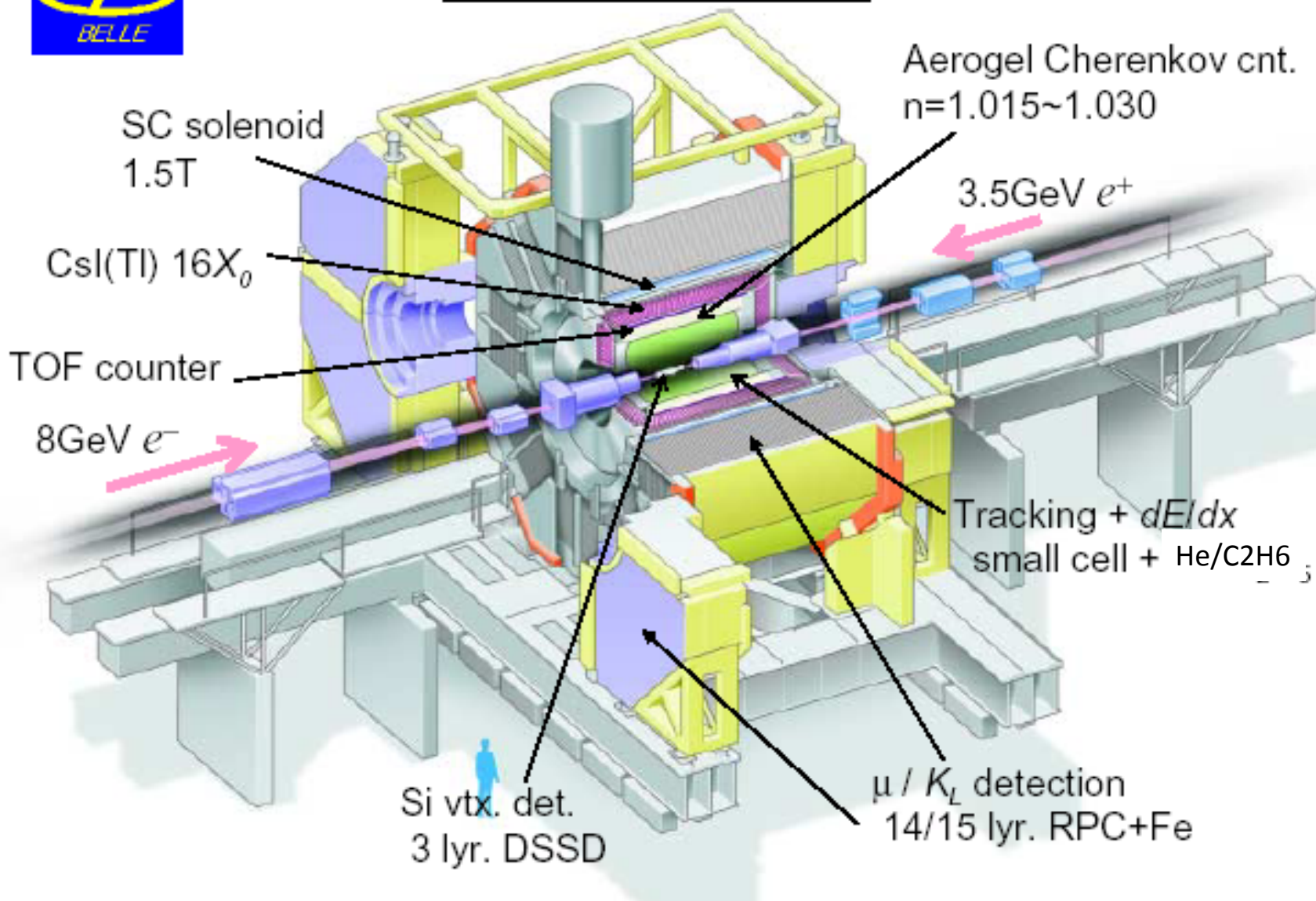


BELLE Detector

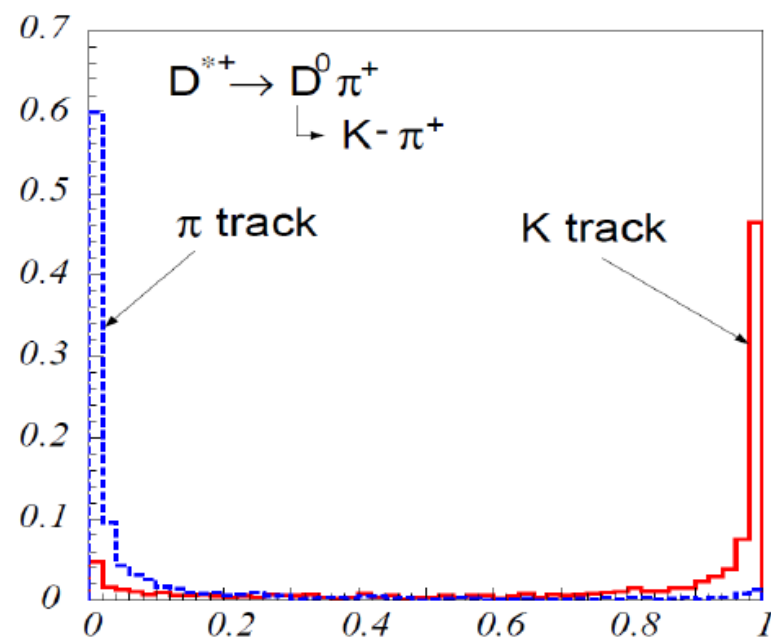
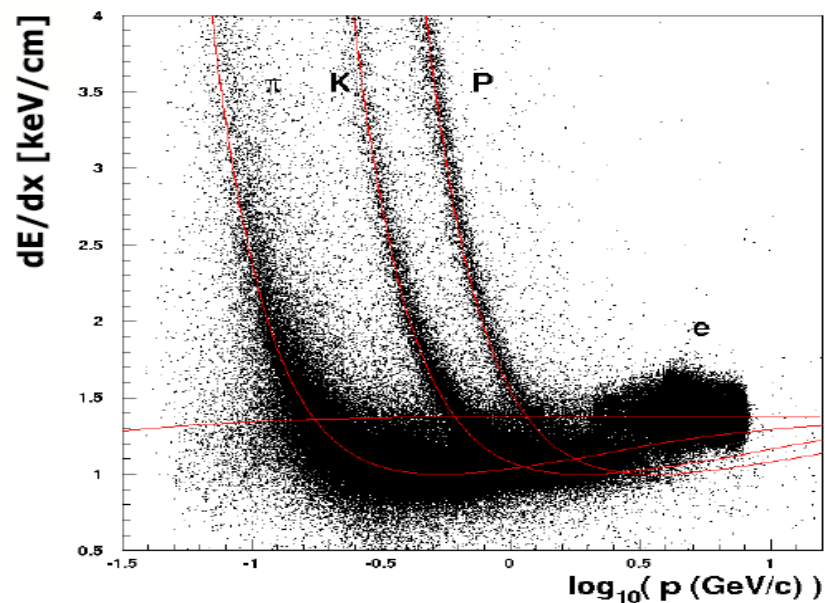
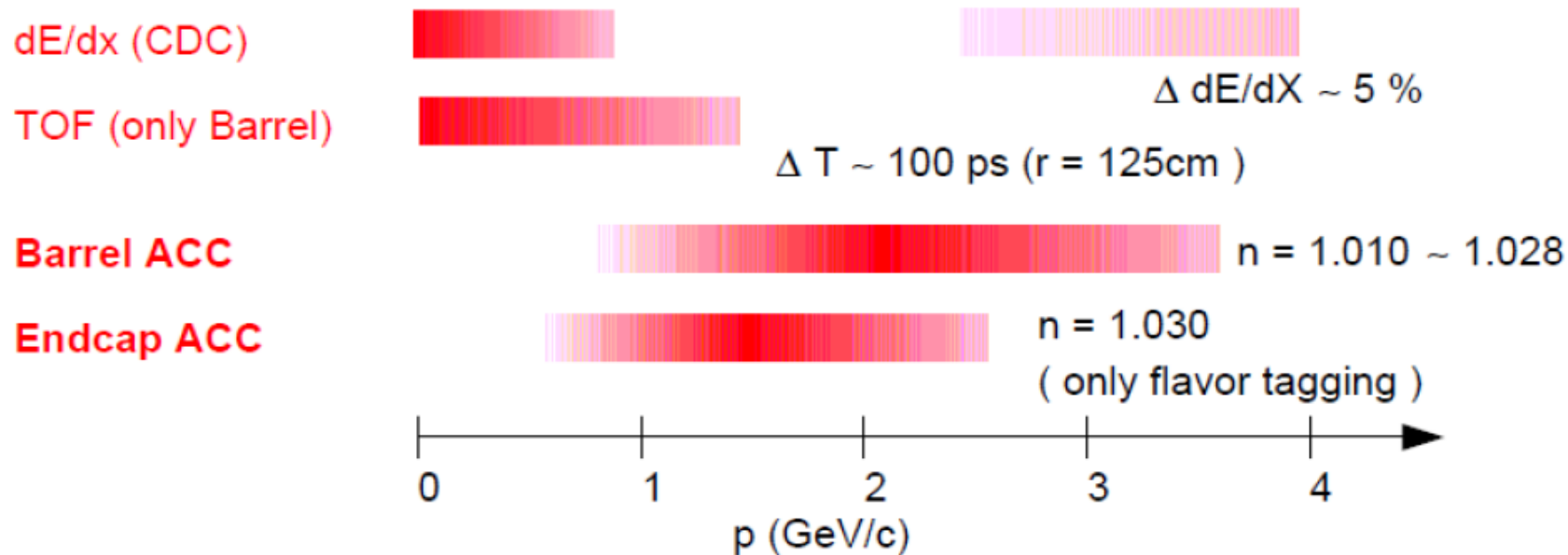




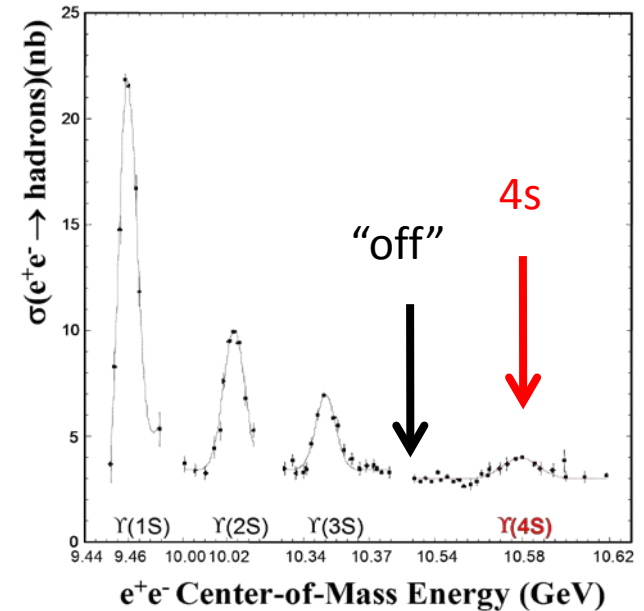
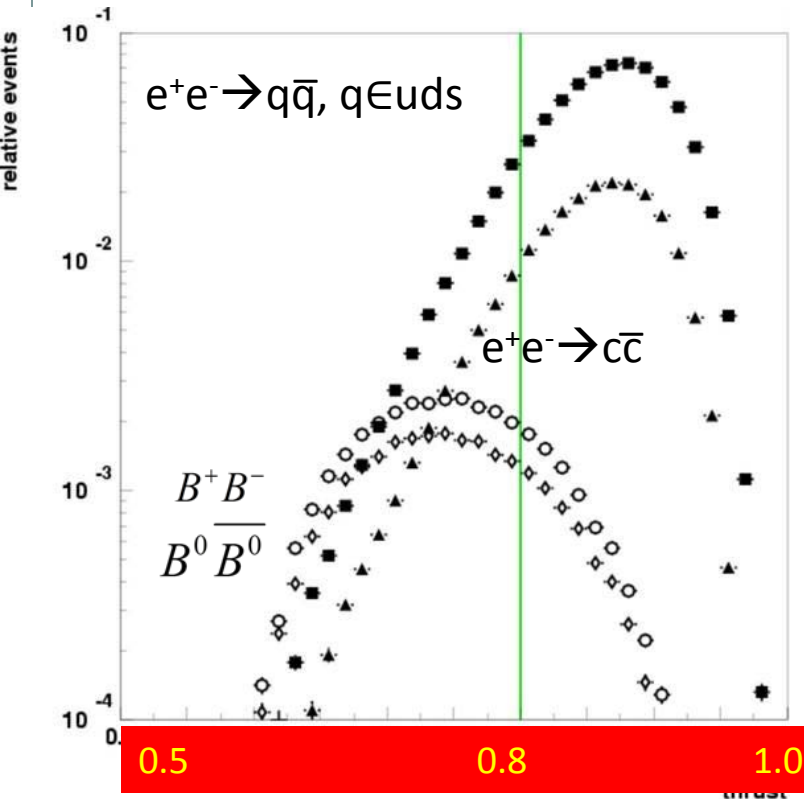
Belle Detector



Large acceptance, good tracking and particle identification!



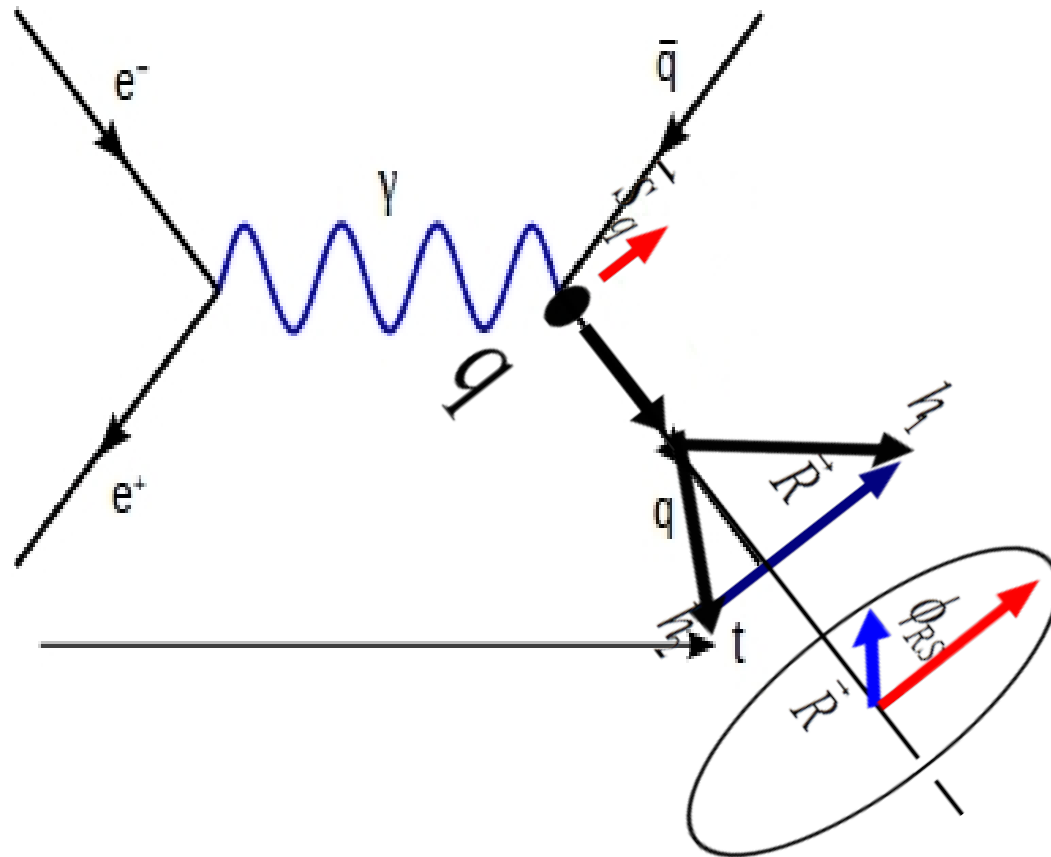
Measuring Light Quark Fragmentation Functions on the $\Upsilon(4S)$ Resonance



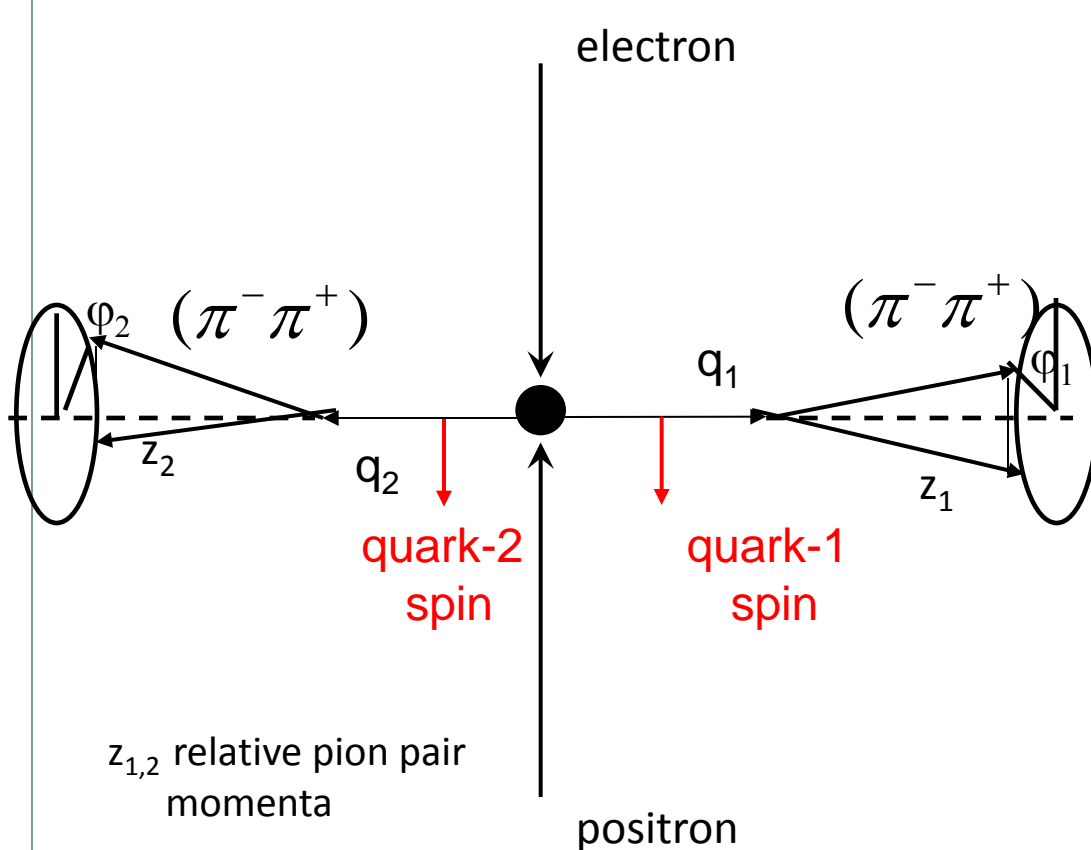
- small B contribution (<1%) in high thrust sample
- >75% of X-section continuum under $\Upsilon(4S)$ resonance
- $\sim 100 \text{ fb}^{-1} \rightarrow \sim 1000 \text{ fb}^{-1}$

$$\text{Thrust: } T = \frac{\sum_i |p_i \cdot \hat{n}|}{\sum_i |p_i|}$$

How to Measure Spin Dependent Fragmentation Functions in unpolarized $e^+ e^-$



Measuring transverse spin dependent di-Hadron Correlations In unpolarized e^+e^- Annihilation into Quarks



Interference effect in e^+e^- quark fragmentation will lead to azimuthal asymmetries in di-hadron correlation measurements!

Experimental requirements:

- Small asymmetries \rightarrow very large data sample!
- Good particle ID to high momenta.
- Hermetic detector

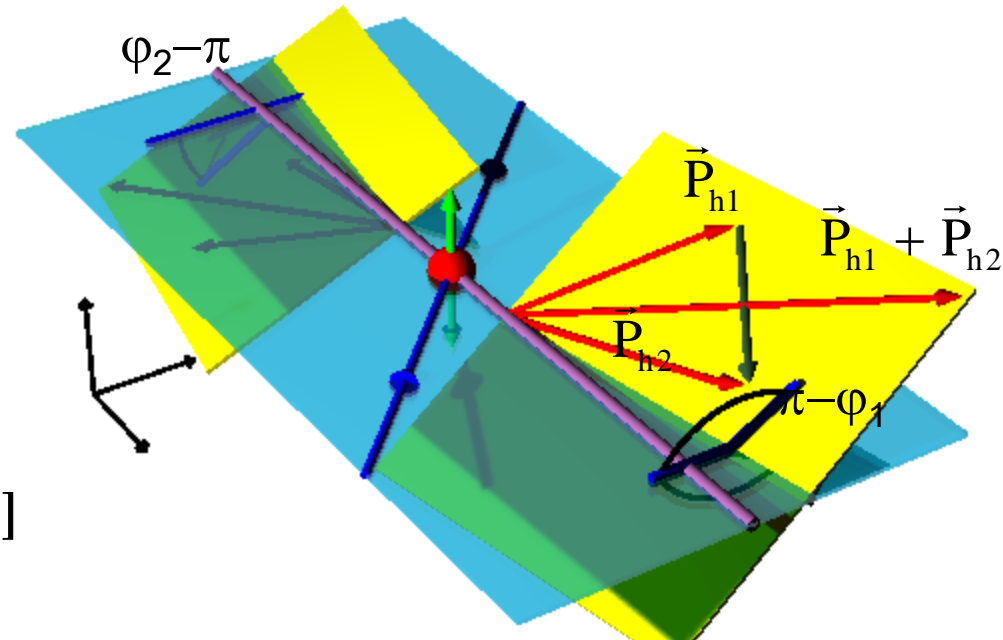
$$A \propto H_1^\perp(z_1, m_1) \bar{H}_1^\perp(z_2, m_2) \cos(\phi_1 + \phi_2)$$



Interference Fragmentation Function from di-Hadron Pair Correlations

- $e^+e^- \rightarrow (\pi^+\pi^-)_{\text{jet1}}(\pi^+\pi^-)_{\text{jet2}}X$
- Find pion pairs in opposite hemispheres
- Observe angles $\phi_1 + \phi_2$ between the event-plane (beam, jet-axis) and the two two-pion planes.
- Theoretical guidance by papers of Boer, Jakob, Radici [PRD 67, (2003)] and Artru, Collins [ZPhysC69(1996)]
- Early work by Collins, Heppelmann, Ladinsky [NPB420(1994)]

$$A \propto H_1^{\angle}(z_1, m_1) \overline{H}_1^{\angle}(z_2, m_2) \cos(\varphi_1 + \varphi_2)$$

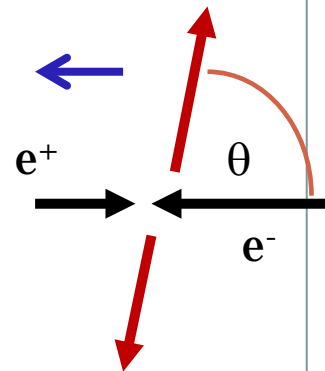


Model predictions by:

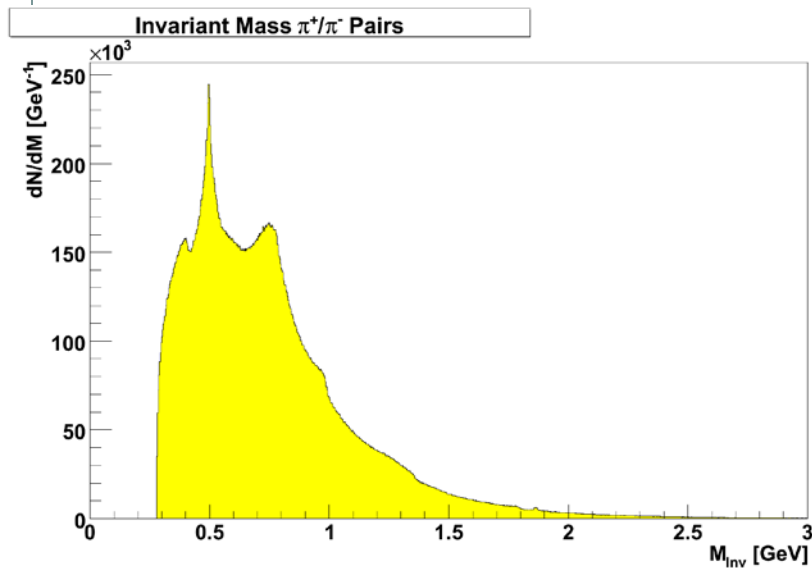
Transverse Spin Dependent FFs: Cuts and Binning

- Full off-resonance and on-resonance data
(7-55): $\sim 73 \text{ fb}^{-1} + 588 \text{ fb}^{-1}$
- Visible energy $> 7 \text{ GeV}$, exclusion of $\tau \rightarrow \pi^- \pi^+ \pi^- \nu_\tau$
- PID: Purities in for di-pion pairs $> 90\%$
- Same Hemisphere cut within pair ($\pi^+ \pi^-$), opposite hemisphere between pairs
- All 4 hadrons in barrel region: $-0.6 < \cos(\theta) < 0.9$
- Thrust axis in central area: cosine of thrust axis around beam < 0.75
- Thrust > 0.8 to remove B-events $\rightarrow < 1\%$ B events in sample
- $z_{\text{had1, had2}} > 0.1$
- $z_1 = z_{\text{had1}} + z_{\text{had2}}$ and z_2 binning
- $m_{\pi\pi 1}$ and $m_{\pi\pi 2}$ binning
- $m_{\pi\pi 1}, z_1$ binning

T-spin projection:
 $\sin^2(\theta) / (1 + \cos(\theta))^2$



Asymmetry extraction



- Build normalized yields:

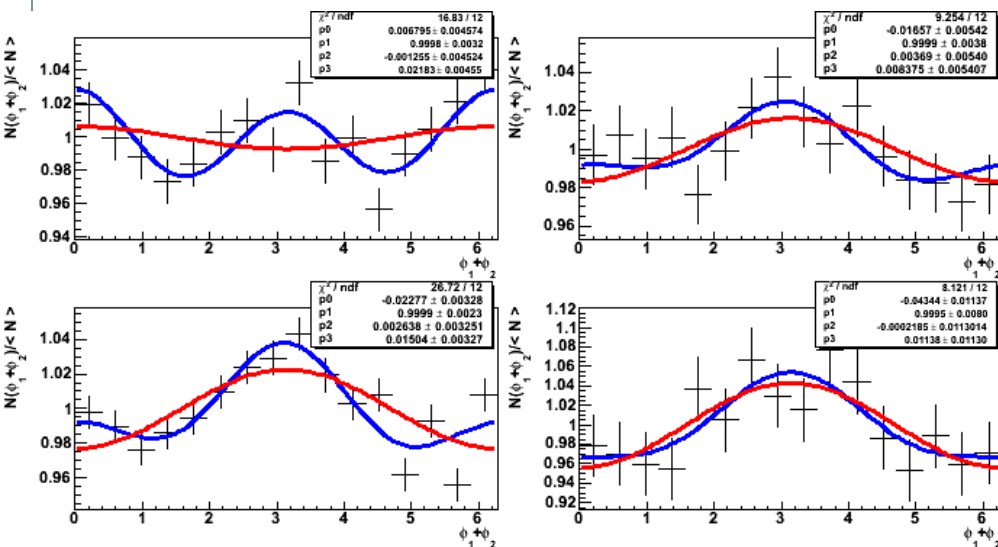
$$\frac{N(\phi_1 + \phi_2)}{\langle N \rangle},$$

- Fit with:

$$a_{12} \cos(\phi_1 + \phi_2) + b_{12}$$

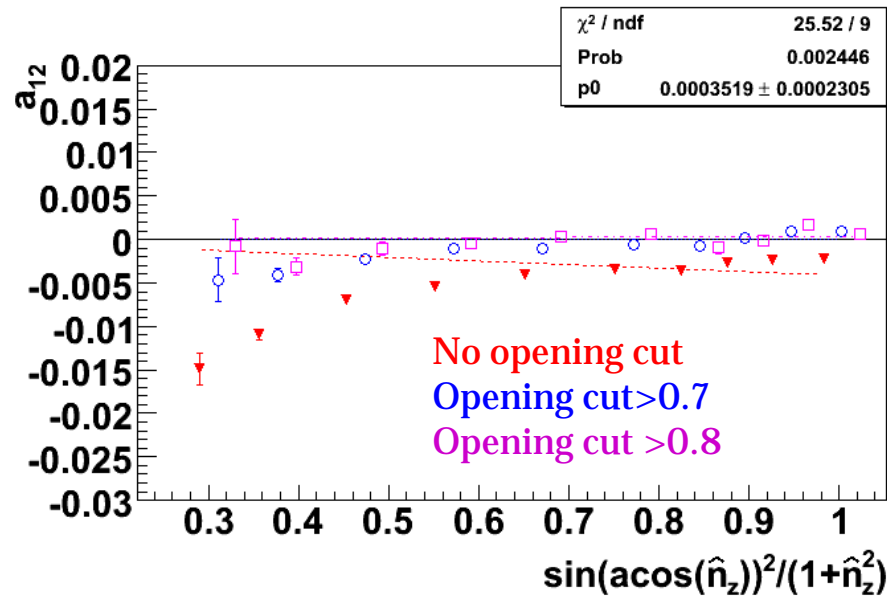
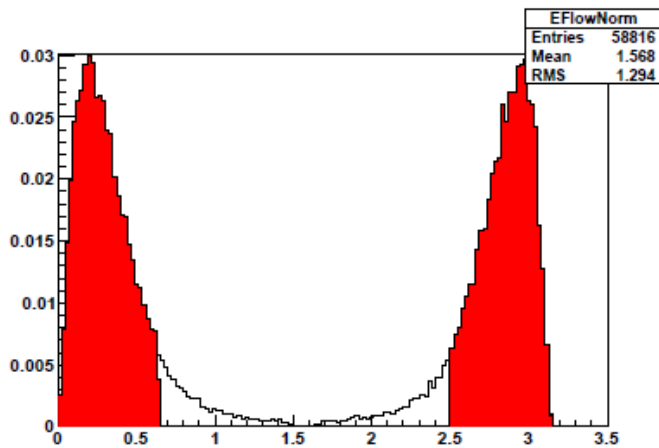
or

$$a_{12} \cos(\phi_1 + \phi_2) + b_{12} + c_{12} \cos 2(\phi_1 + \phi_2) + d_{12} \sin(\phi_1 + \phi_2)$$



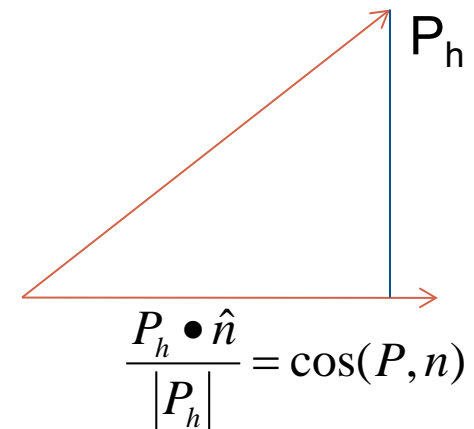
Amplitude a_{12} directly measures (IFF) x (-IFF) (no double ratios)

Zero tests: MC

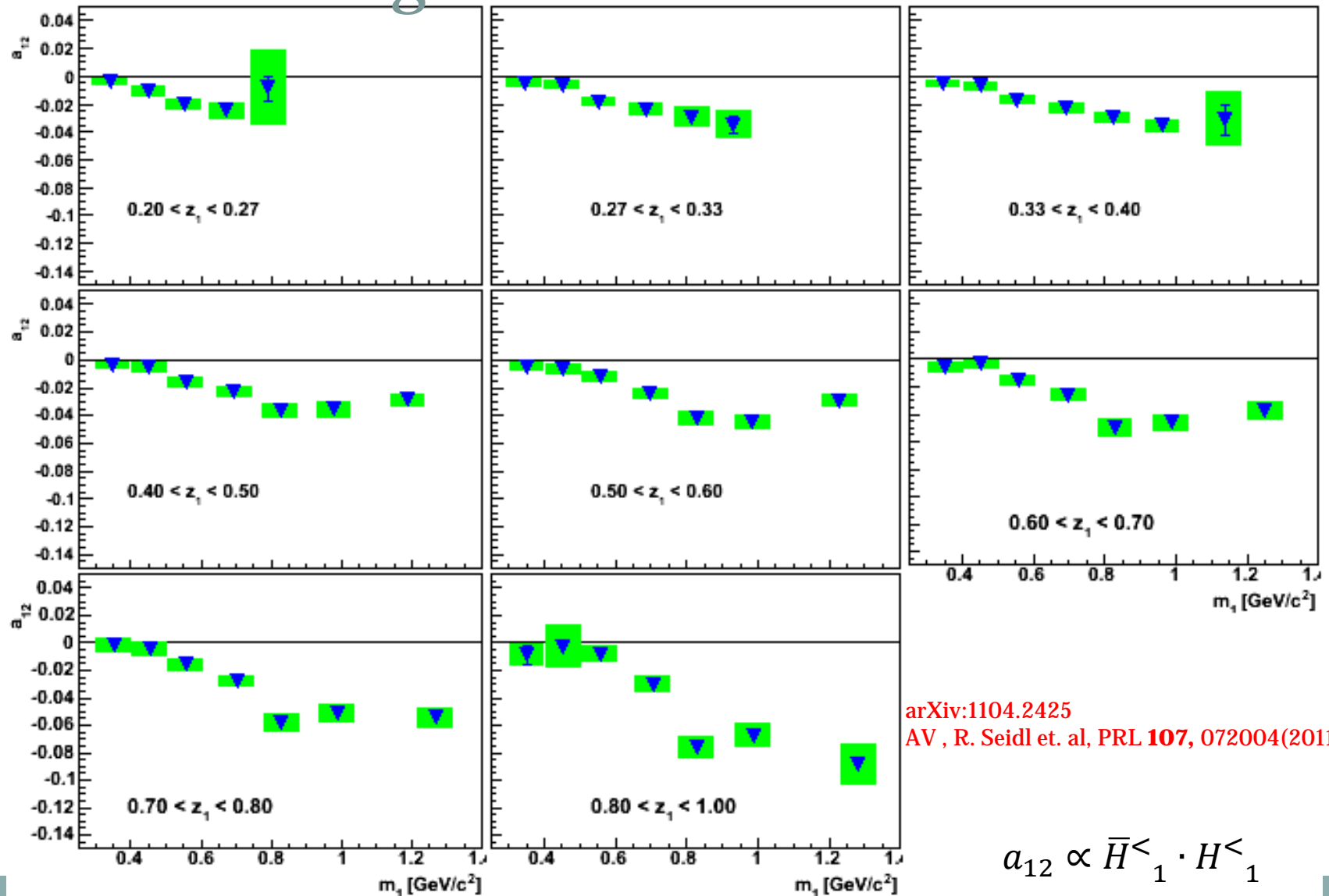


Energy flow with opening cut of 0.8

- A small asymmetry seen due to acceptance effect
- Mostly appearing at boundary of acceptance
- Opening cut in CMS of 0.8 (~37 degrees) reduces acceptance effect to the sub-per-mille level



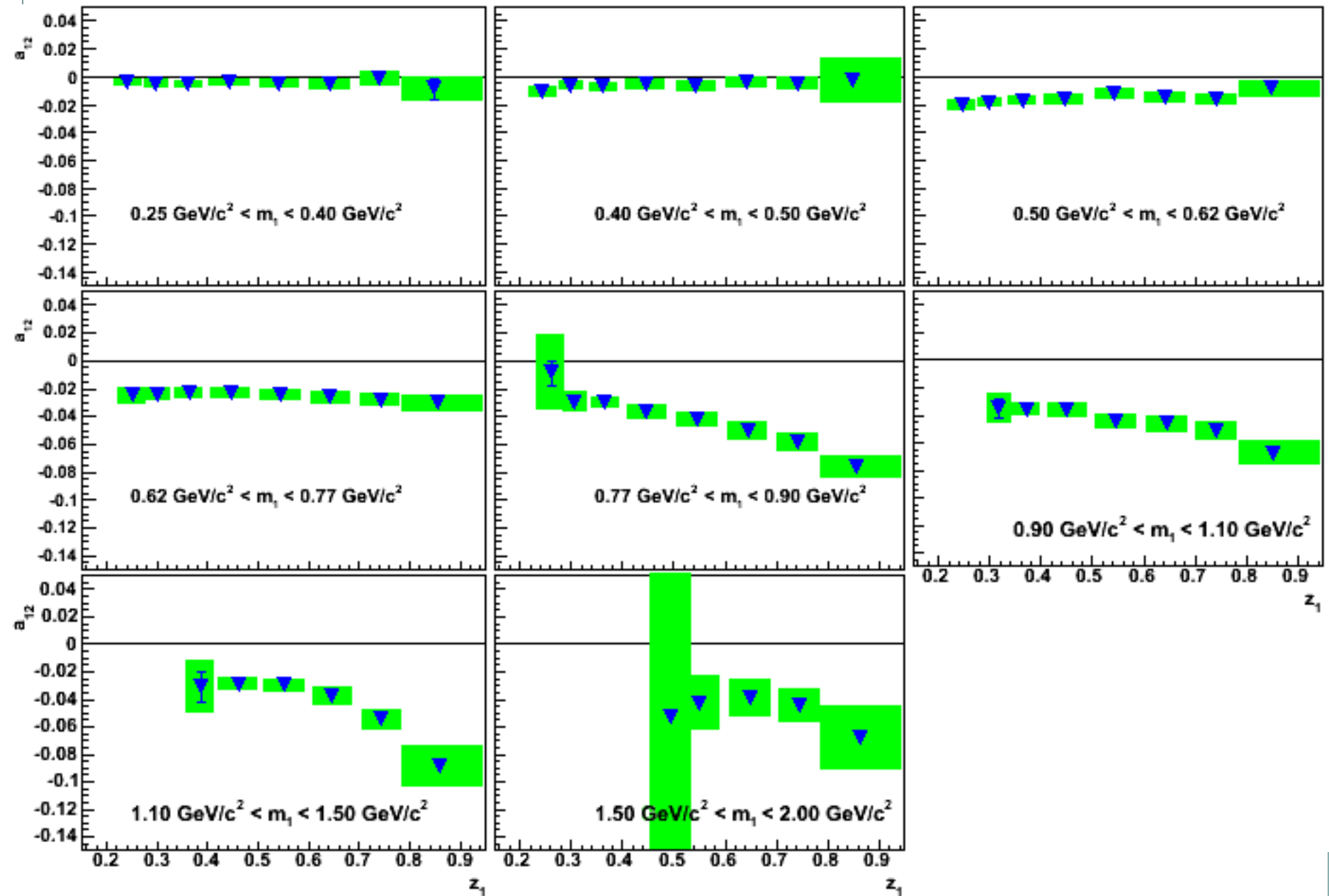
First measurement of Interference Fragmentation Function



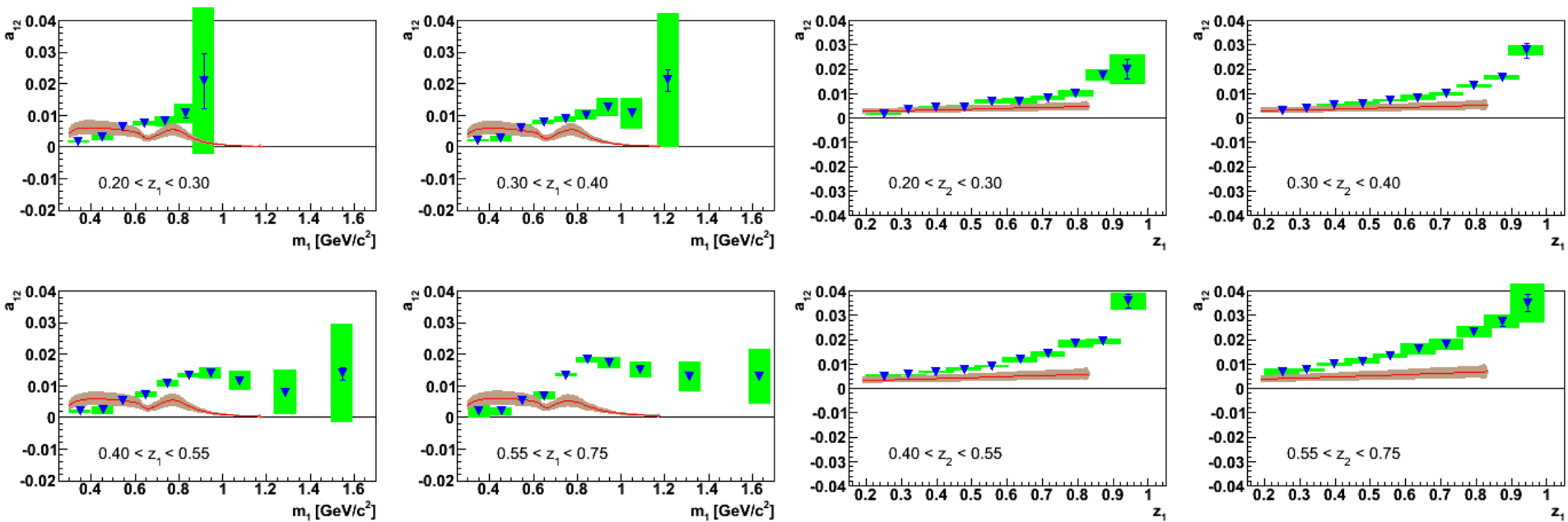
arXiv:1104.2425
 AV, R. Seidl et. al, PRL **107**, 072004(2011)

$$a_{12} \propto \bar{H}_1^< \cdot H_1^<$$

$(m_1 \times z_1)$ Binning



Comparison to theory predictions



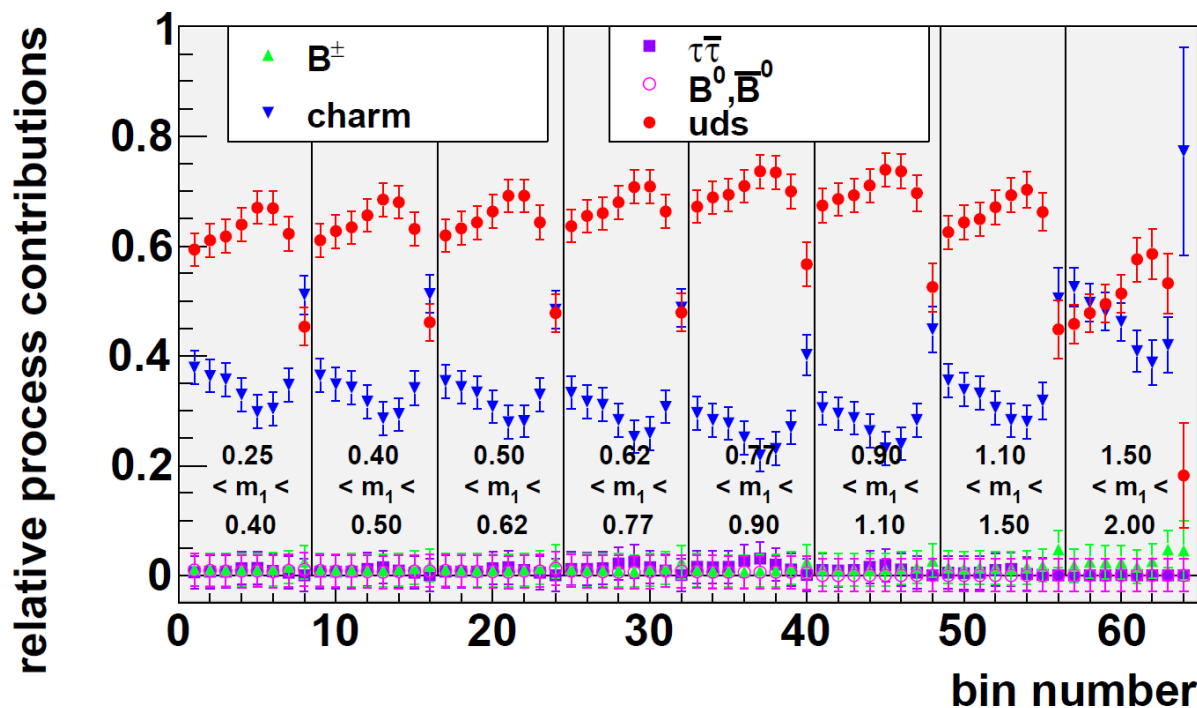
Red line: theory prediction + uncertainties
 Blue points: data

- Mass dependence : Magnitude at low masses comparable, high masses significantly larger (some contribution possibly from charm)
- Z dependence : Rising behavior steeper

Subprocess contributions (MC)

8x8 m_1 m_2 binning

36



tau contribution (only significant at high z)

charged B (<5%, mostly at higher mass)

Neutral B (<2%)

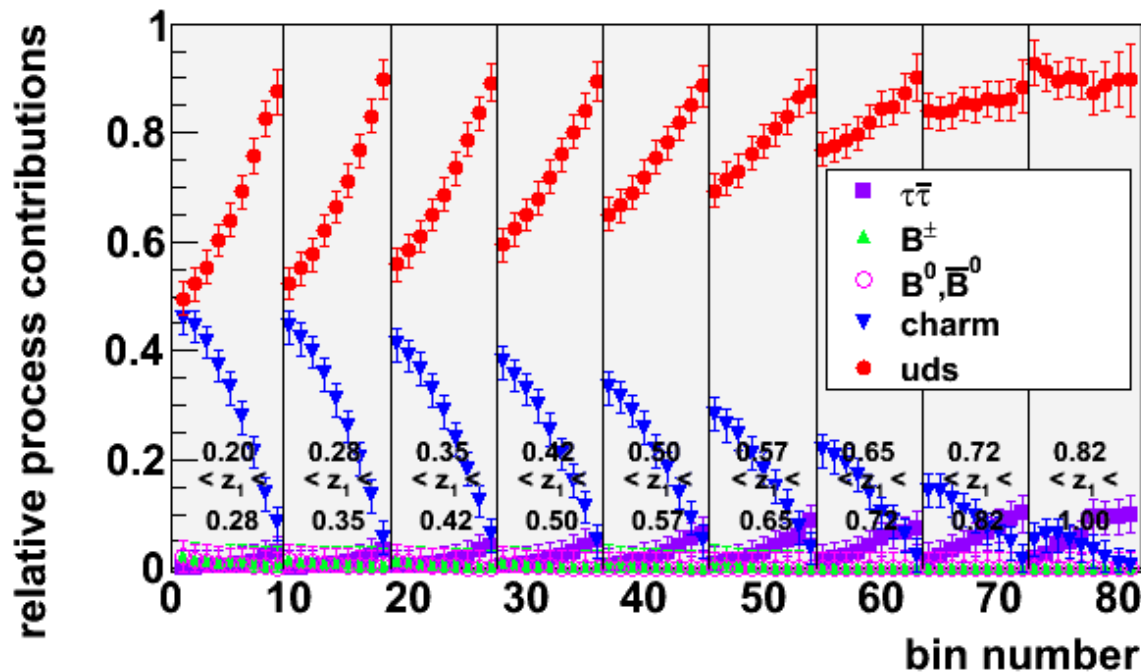
charm (20-60%, mostly at lower z)

uds (main contribution)

Subprocess contributions (MC)

9x9 z_1 z_2 binning

37



tau contribution (only significant at high z)

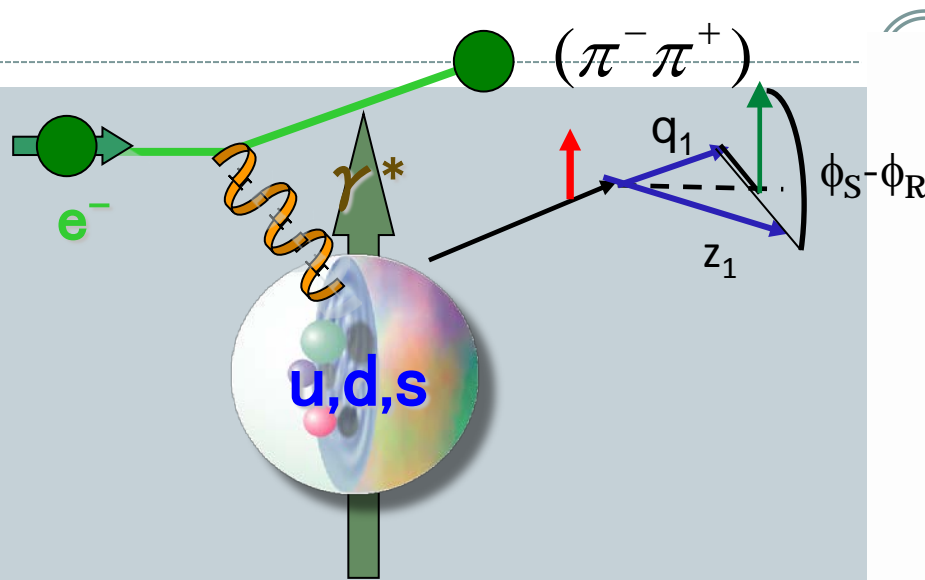
charged B(<5%, mostly at higher mass)

Neutral B (<2%)

charm(20-60%, mostly at lower z)

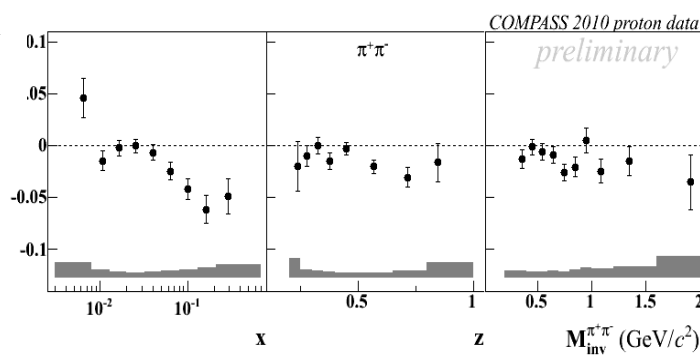
uds (main contribution)

COMPASS 2004 Setup



$$\frac{\sigma^\uparrow - \sigma^\downarrow}{\sigma^\uparrow + \sigma^\downarrow} (\phi_S - \phi_R) = A_{UT} \sin(\phi_S - \phi_R)$$

$$A_{UT} \propto h_1 \cdot H_1^<$$



two stages spectrometer

Large Angle Spectrometer (SM1),

Small Angle Spectrometer (SM2)

MuonWall

E/HCAL

MuonWall

E/HCAL

RICH

Polarised Target

SM1

SM2

2002-2004: 6LiD (Deuteron)

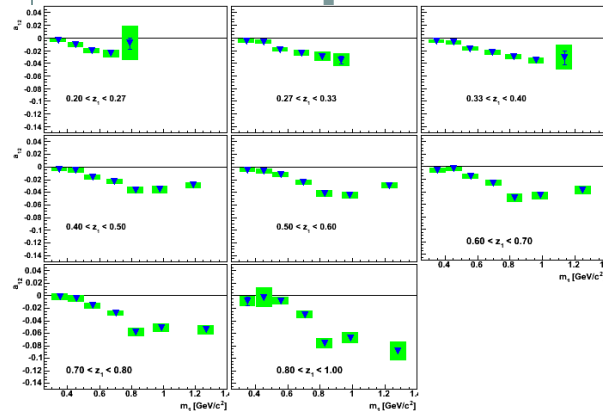
dilution factor $f = 0.38$ polarization $PT = 50\%$

>2005 NH3 (proton)

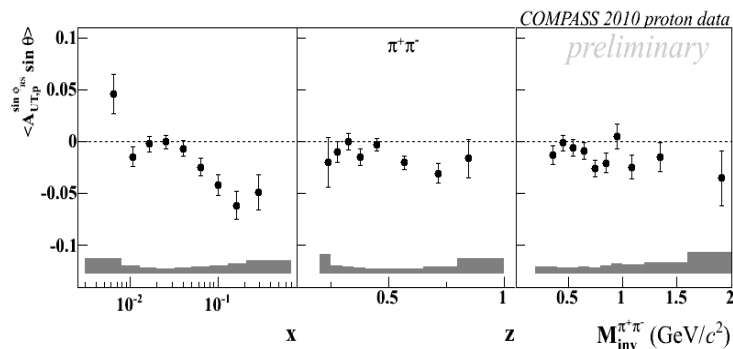
3 target cells with opposite polarization, 90% polarization, 16% dilution

- high energy beam
- Large angular acceptance
- Broad kinematical range

Measurement at Belle leads to first point by point extraction of Transversity

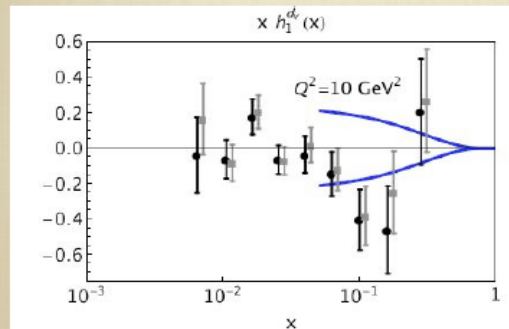
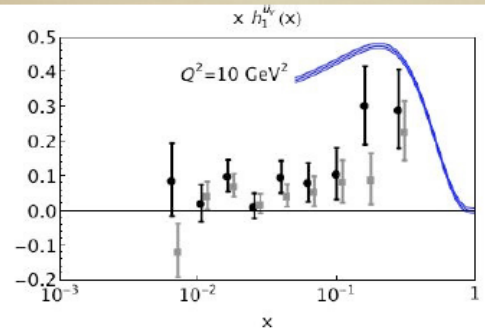


$$a_{12} \propto H_1^< \cdot H_1^<$$



$$A_{UT} \propto h_1 \cdot H_1^<$$

M. Radici at FF workshop, RIKEN, 11/2012
See also: Courtoy: Phys. Rev. Lett.
107:012001,2011



Future Plans at
Star/Belle:

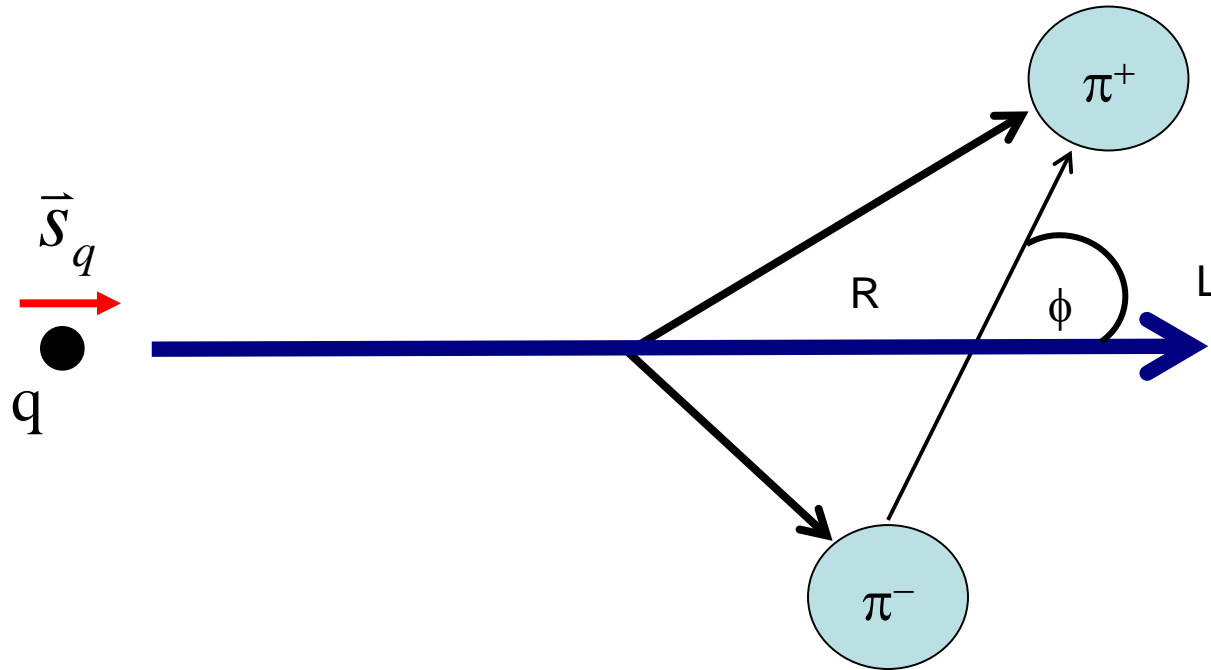
Better sensitivity to d
transversity
From $\pi^0/\pi^{+/-}$
combinations

Increase x range

Is Soffer Bound
violated?

$$h(x) < |f(x) + g(x)| / 2$$

Jet Handedness



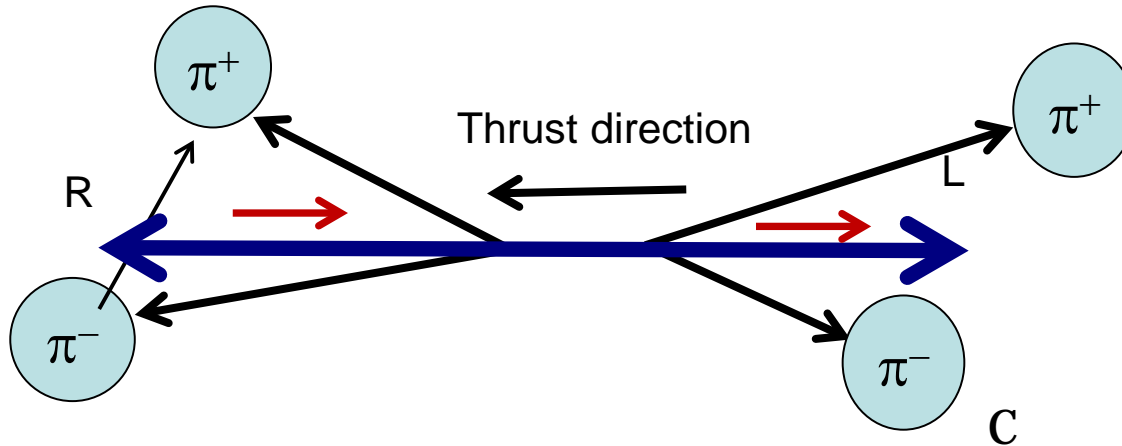
$$\text{Handedness: } \frac{(\vec{k}_+ \times \vec{k}_-) \cdot \vec{t}}{|\vec{k}_+| |\vec{k}_-|} \Rightarrow \text{L/R}$$

$$= \sin \Phi > 0$$

$$\text{Jet handedness: } \frac{N_R - N_L}{N_R + N_L}$$

Handedness Correlations

- Handedness Correlations expected to be zero in factorized approach
- Non-zero asymmetries predicted in factorized approach for azimuthal asymmetries sensitive to G_1^\perp
- Several suggestions how interactions with QCD vacuum can lead to non-zero asymmetries



Handedness: $\frac{(\vec{k}_+ \times \vec{k}_-) \cdot \vec{t}}{|\vec{k}_+| |\vec{k}_-|} >? 0 \Rightarrow \text{L/R}$

Jet

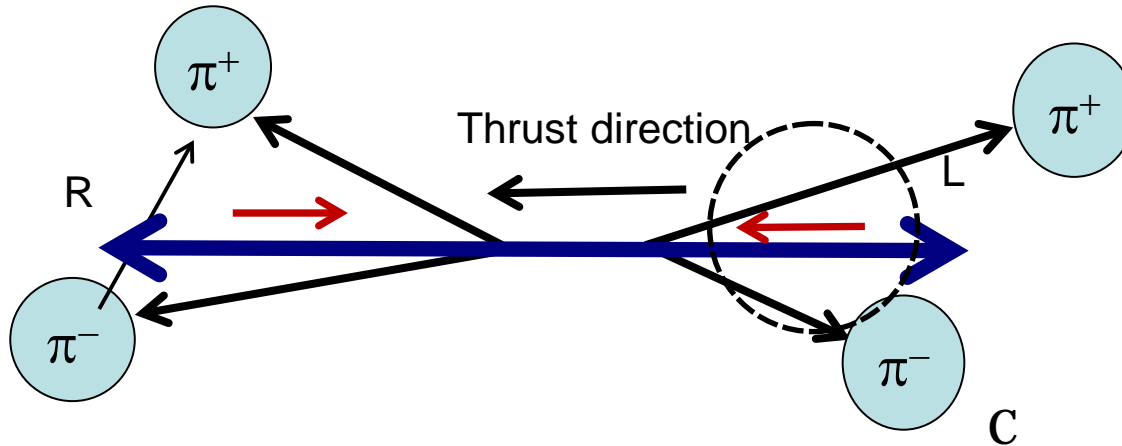


handedness: $\frac{N_R - N_L}{N_R + N_L}$

C: $\frac{N_{RL} + N_{LR} - N_{RR} - N_{LL}}{N_{RL} + N_{LR} + N_{RR} + N_{LL}}$

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Handedness:
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Jet

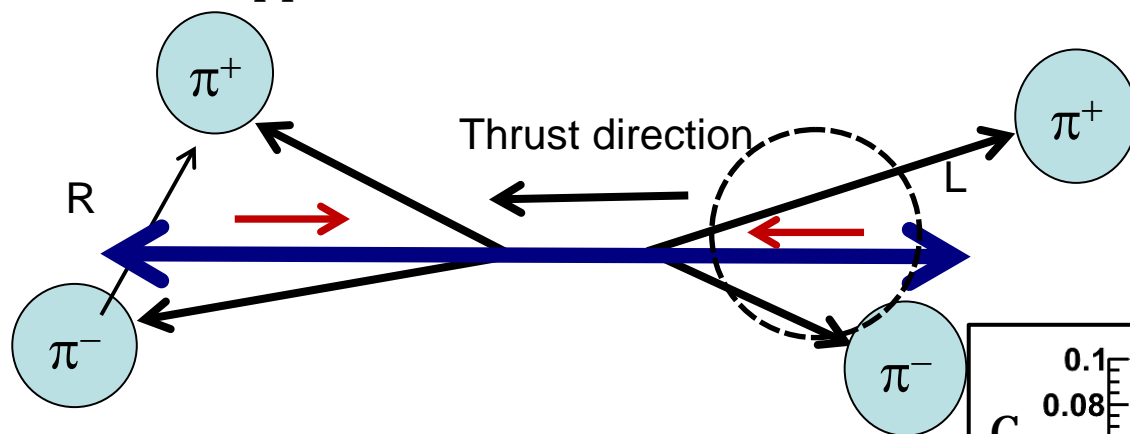


handedness:
$$\frac{N_R - N_L}{N_R + N_L}$$

C:
$$\frac{N_{RL} + N_{LR} - N_{RR} - N_{LL}}{N_{RL} + N_{LR} + N_{RR} + N_{LL}}$$

Handedness Correlations

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- Several suggestions how interactions with QCD vacuum can lead to non-zero asymmetries
- SLD: Upper bound from 90k hadronic Z events: 7%



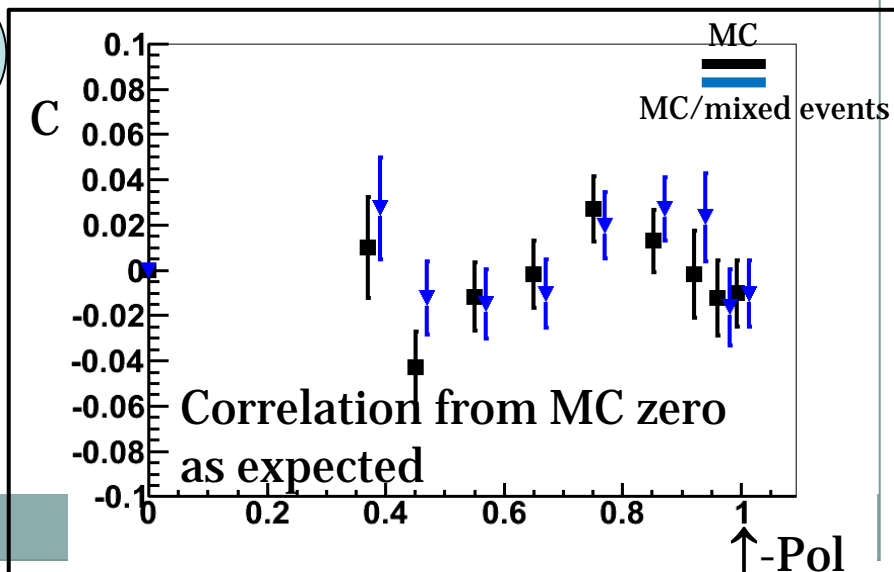
$$\text{Handedness: } \frac{(\vec{k}_+ \times \vec{k}_-) \cdot \vec{t}}{|\vec{k}_+| |\vec{k}_-|} >? 0 \Rightarrow \text{L/R}$$

Jet



$$\text{handedness: } \frac{N_R - N_L}{N_R + N_L}$$

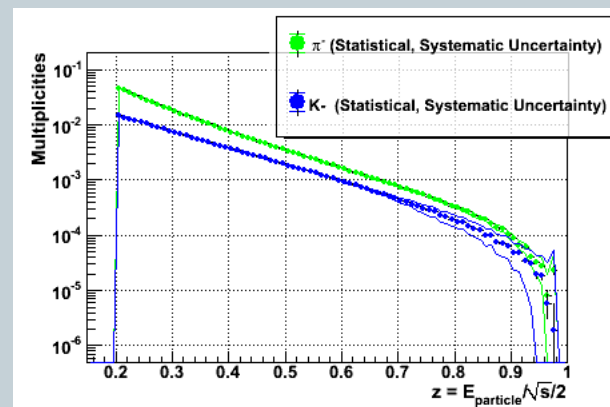
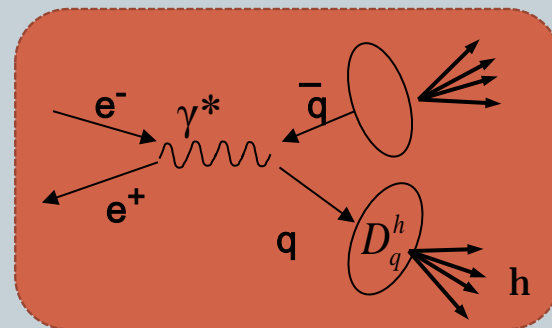
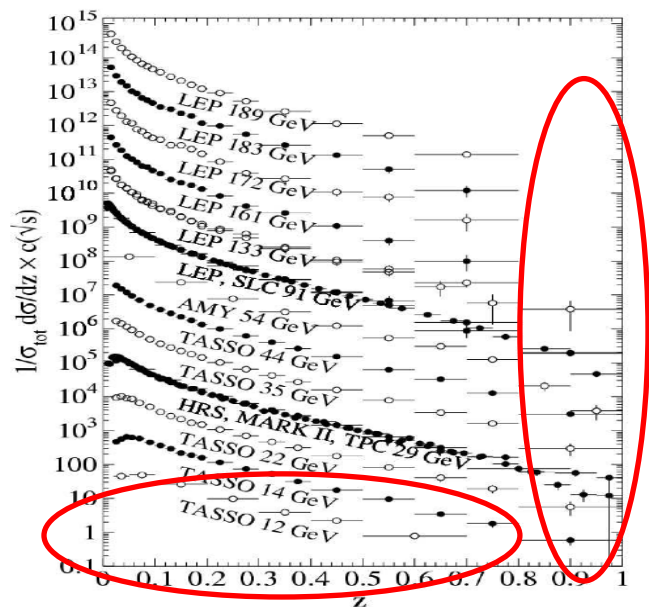
$$C: \frac{N_{RL} + N_{LR} - N_{RR} - N_{LL}}{N_{RL} + N_{LR} + N_{RR} + N_{LL}}$$



Unpolarized Fragmentation Functions

- Precise knowledge of upol. FFs necessary for virtually all SIDIS measurements

Lack of data at high z , lower CMS

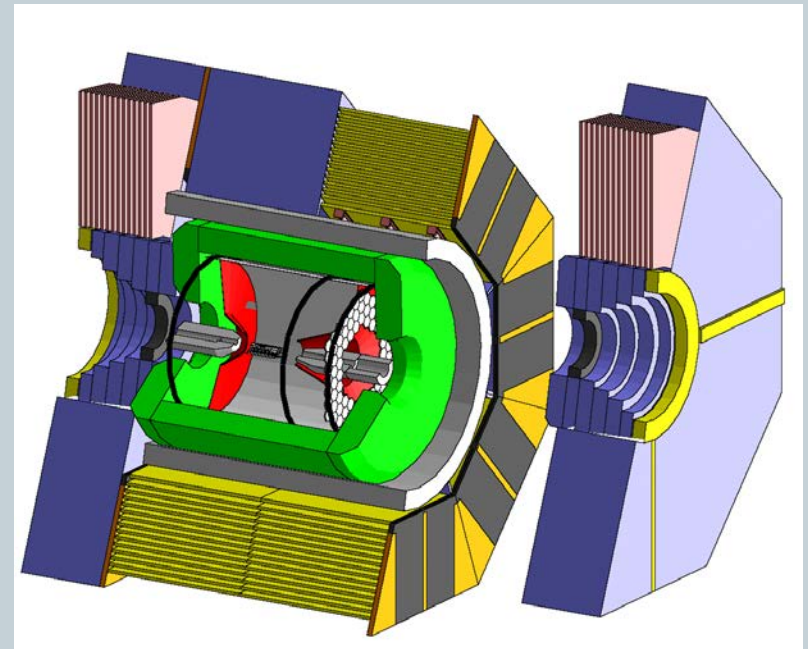
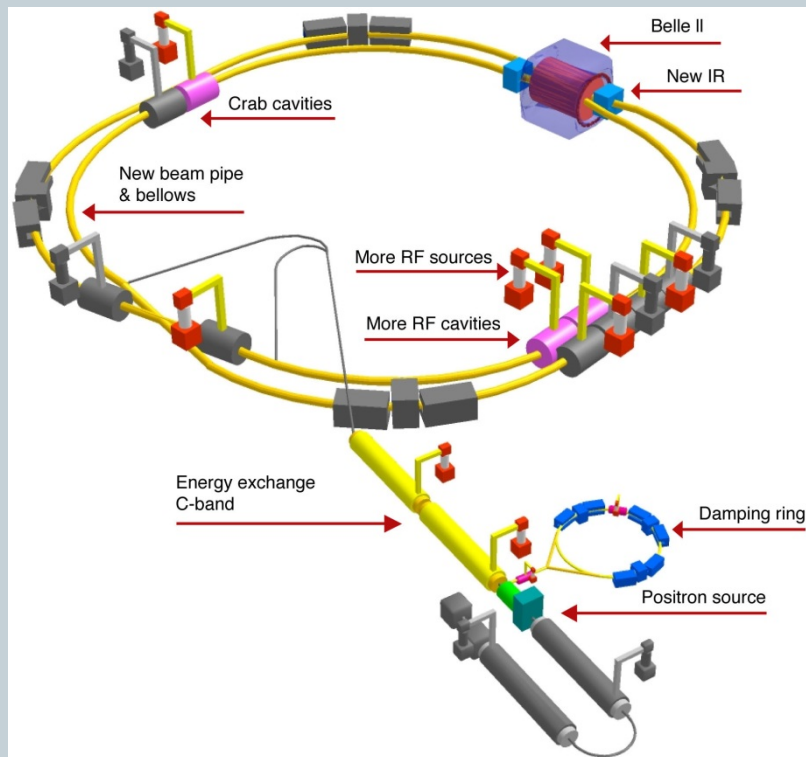


- π^0 , η fragmentation function under way
- In particular important at RHIC

Submitted to PRL
[arXiv:1301.6183](https://arxiv.org/abs/1301.6183)

M. Leitgab (UIUC)

- Aim: super-high luminosity $\sim 10^{36} \text{ cm}^{-2} \text{ s}^{-1}$ ($\sim 40 \times$ KEK/Belle)
 - Will allow p_T dependent extraction of fragmentation functions
- Upgrades of Accelerator (Microbeams + Higher Currents) and Detector
- Significant US contribution



<http://belle2.kek.jp>

Belle II Detector at SuperKEKB (L x 40)

and IU contributions to Barrel Particle ID

- Barrel PID instrumental for fragmentation function measurements

EM Calorimeter:
CsI(Tl), waveform sampling (barrel)
Pure CsI + waveform sampling (end-caps)

e^- (7GeV)

Vertex Detector
2 layers DEPFET + 4 layers DSSD
**Vertex resolution improved by order of magnitude:
Separate charm/uds**

K_L and muon detector:

Resistive Plate Counter (barrel outer layers)

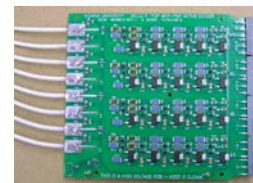
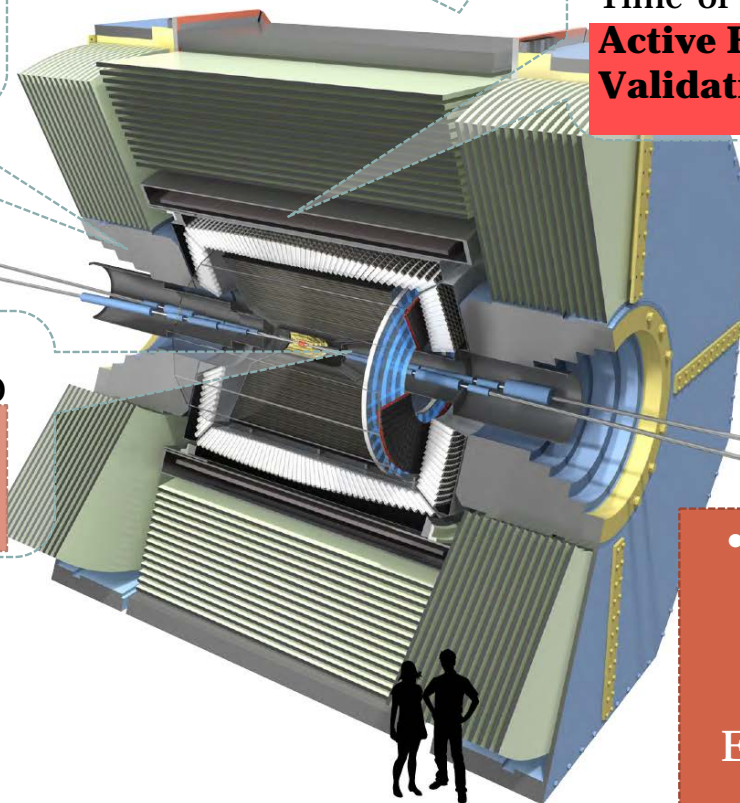
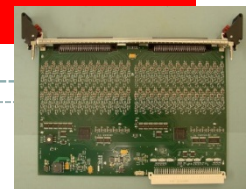
Scintillator + WLSF + MPPC (end-caps, inner 2 barrel layers)

RPC Front End Electronics, Concentrator boards for barrel and endcap scintillator layers

Particle Identification

Time-of-Propagation counter (barrel)

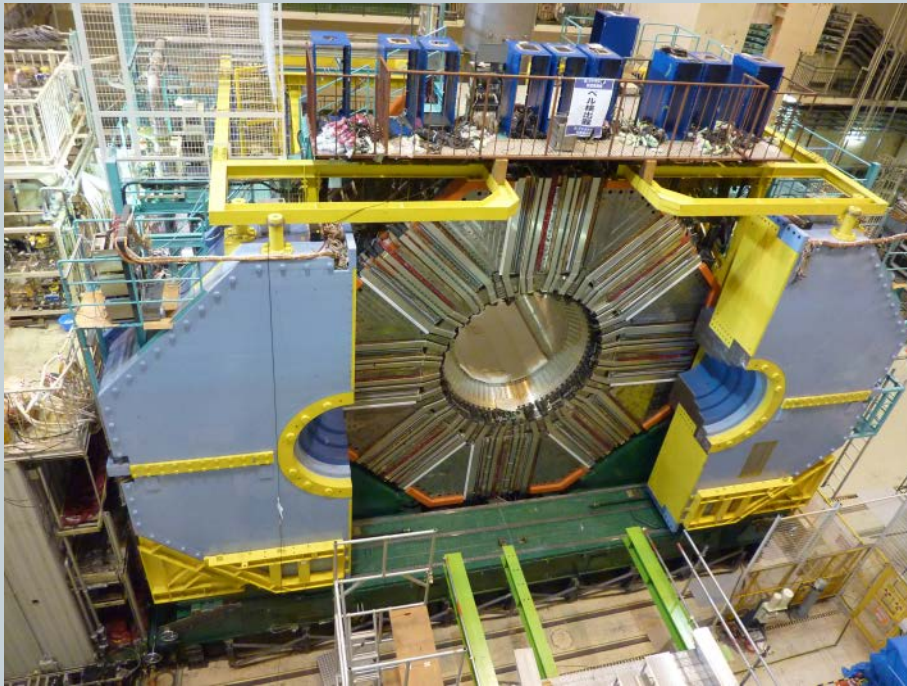
**Active HV Divider board for MCP-PMT
Validation of FPGA code of iTOP**



- RPC test stand at IU to test electronics:
E. Zarndt, S. Arnold



Belle II Status



Summary



- Breakthrough Measurements of Proton Structure underway: How does QCD work inside the Nucleon?
- Di-hadron Correlations best way to access transversity in p+p, SIDIS needed to describe spin structure of the proton, derive tensor charge
- Corresponding Fragmentation Functions measured at Belle
 - IFF, Collins in Pions, Kaons (underway), spin averaged single, di-hadron Fragmentation functions,



- Outlook
 - **Belle II:** Continuation of FF measurements with improved Kaon ID and vertex reconstruction
 - Use charm rejection
 - Probe QCD vacuum polarization
 - Measure transverse momentum dependent spin dependent and spin averaged fragmentation functions
 - Precision measurements at Belle (II) **crucial** for forthcoming measurements at BNL, Jlab, CERN



THANK YOU!

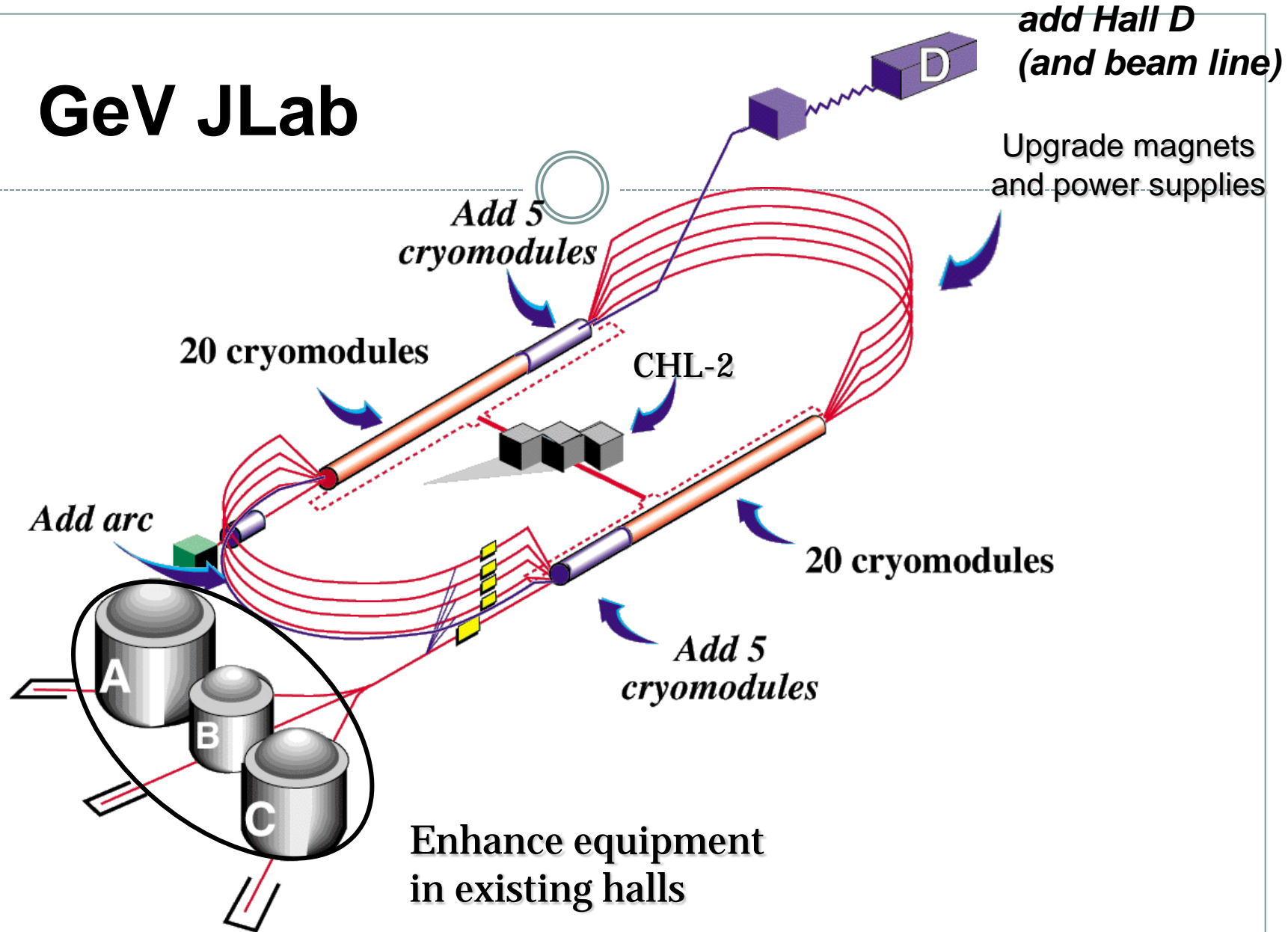
Questions?



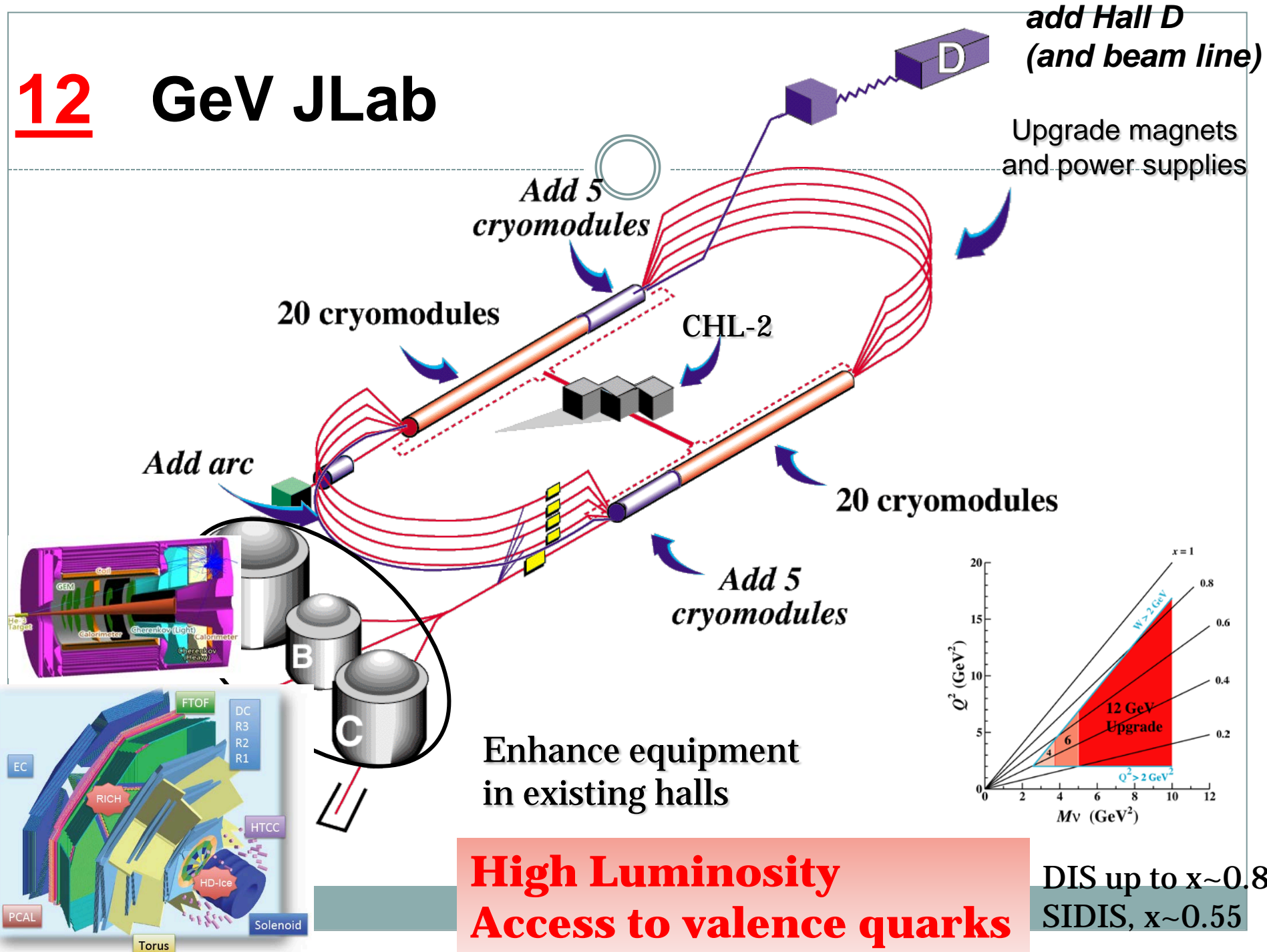
- **Backup**

12

GeV JLab

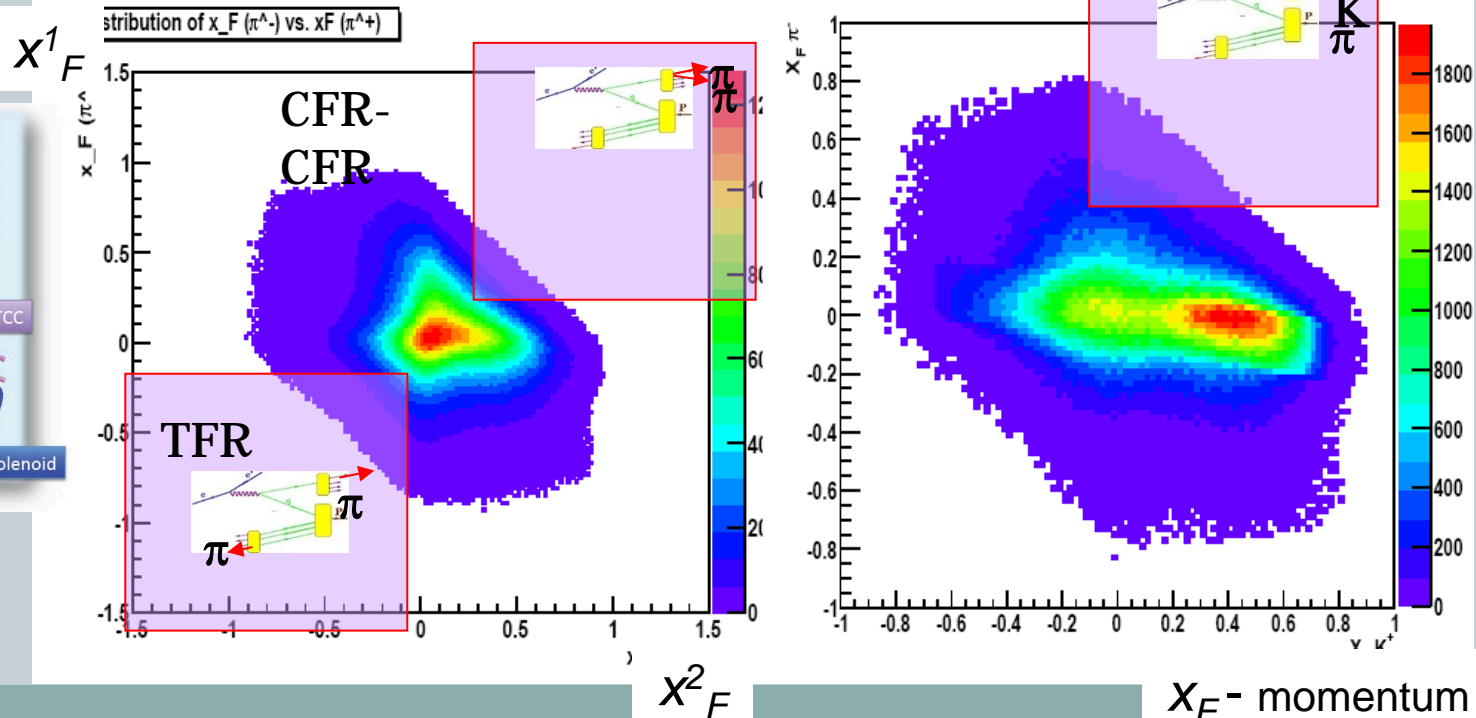
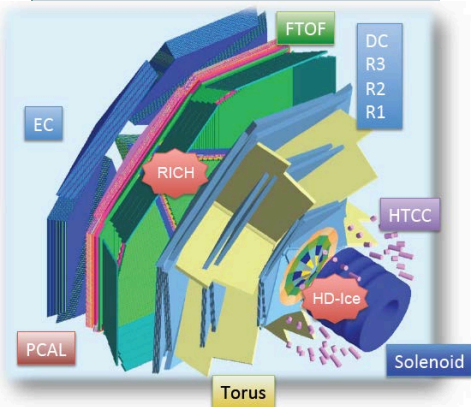
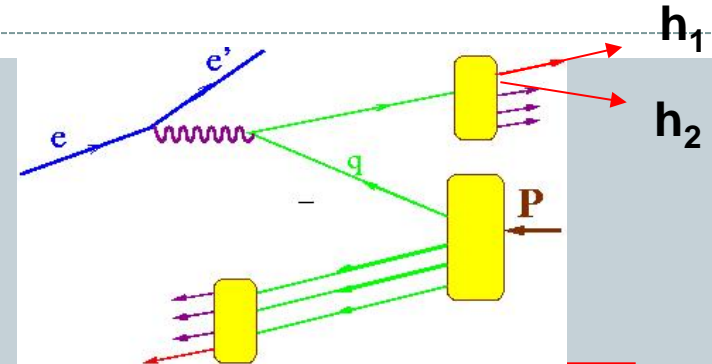


12 GeV JLab



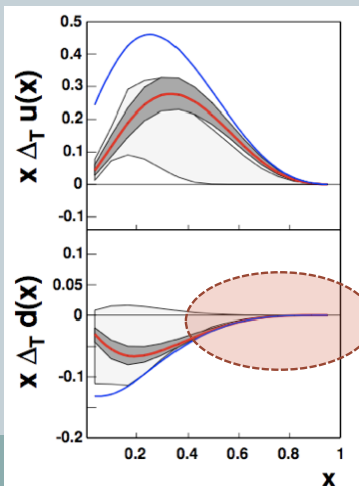
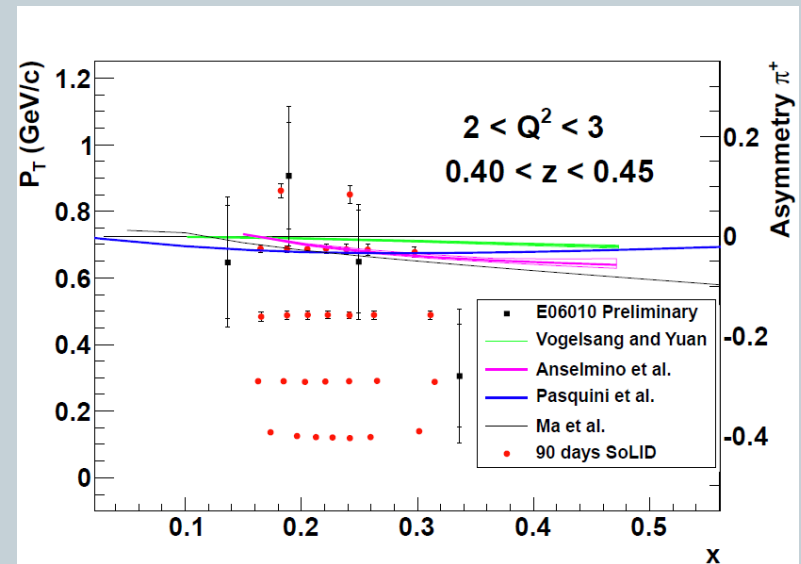
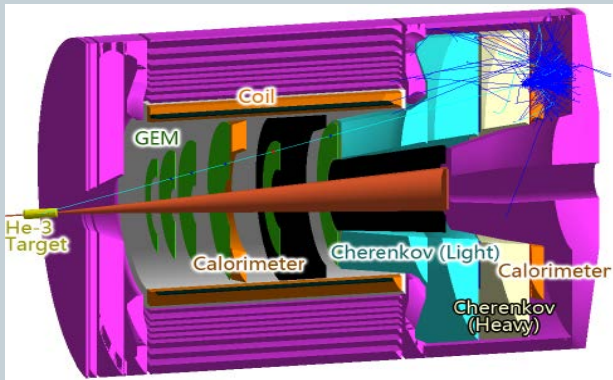
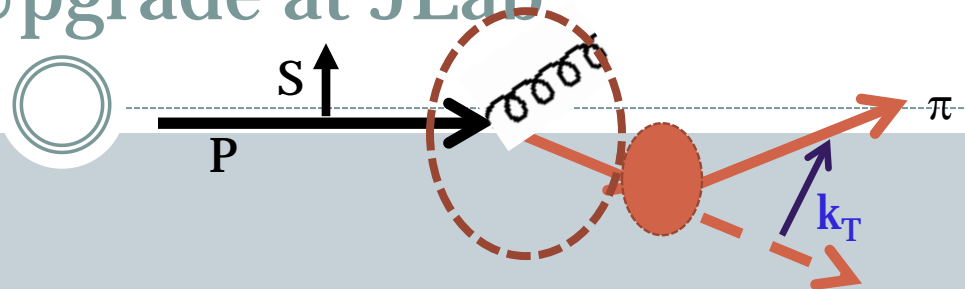
Di-hadron Correlations at CLAS

- Di-hadron correlations at CLAS to extract higher twist distribution functions and transversity (with new target)
- Need for πK IFF to exclude target Fragmentation (Belle!)



Plots from H. Avakian
 Dihadron sample defined by SIDIS cuts+ $x_F > 0$ (CFR) for both hadrons

Transversity at high x from polarized He3 at SoLID with 12 GeV Upgrade at JLab



- Precise measurement of p_T dependent Collins effect
 - Needs precise measurement of Collins and spin averaged p_T dependent fragmentation functions

Collins Extraction of Transversity: model dependence from Transverse Momentum Dependences!



$$A_{UT}^{Collins} = \frac{\sum_q e_q^2 \int d\phi_S d\phi_h d^2 k_\perp \overset{\text{transversity}}{h(x, \vec{k}_\perp)} \frac{d(\Delta\sigma)}{dy} \overset{\text{Collins FF}}{H_{1,q}^\perp(z, \vec{p}_\perp) \sin(\phi_S + \phi + \phi_q^h) \sin(\phi_S + \phi_h)}}{\sum_q e_q^2 \int d\phi_S d\phi_h d^2 k_\perp \underset{\text{quark pdf}}{q(x, \vec{k}_\perp)} \frac{d(\Delta\sigma)}{dy} \underset{\text{hadron FF}}{D_q^h(z, \vec{p}_\perp)}}$$

\vec{k}_\perp *transverse quark momentum in nucleon*

\vec{p}_\perp *transverse hadron momentum in fragmentation*

Anselmino, Boglione, D'Alesio,
Kotzinian, Murgia, Prokudin, Turk
Phys. Rev. D75:054032,2007

The transverse momentum dependencies are still unknown
Need p_T dependent FFs from Belle to extract transversity and test TMD framework